



Large-Scale Evacuation Planning

Actionable Evacuation Plans With Contraflows

Caroline Even, Victor Pillac, Pascal Van Hentenryck
<http://org.nicta.com.au>



Australian Government
**Department of Broadband, Communications
and the Digital Economy**
Australian Research Council

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About NICTA - ORG

- **NICTA**

- 5 research groups
- 3 business teams
- 15 startups



- Optimisation Research Group (**ORG**)
 - ~60 staff & PhDs

Credits



Victor
Pillac

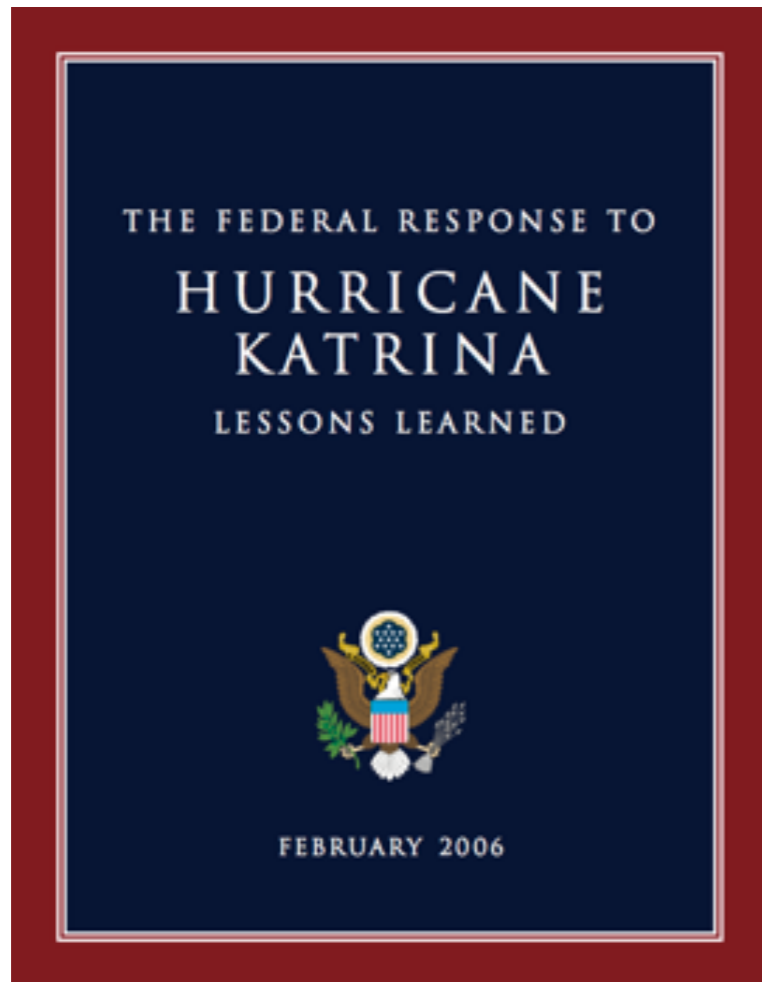


Pascal
Van Hentenryck



Caron
Chen

Disaster management



“The Federal government must develop the capacity to conduct large-scale logistical operations.”
(p 56)

- **Pre-Katrina:**

Focus on providing situational awareness

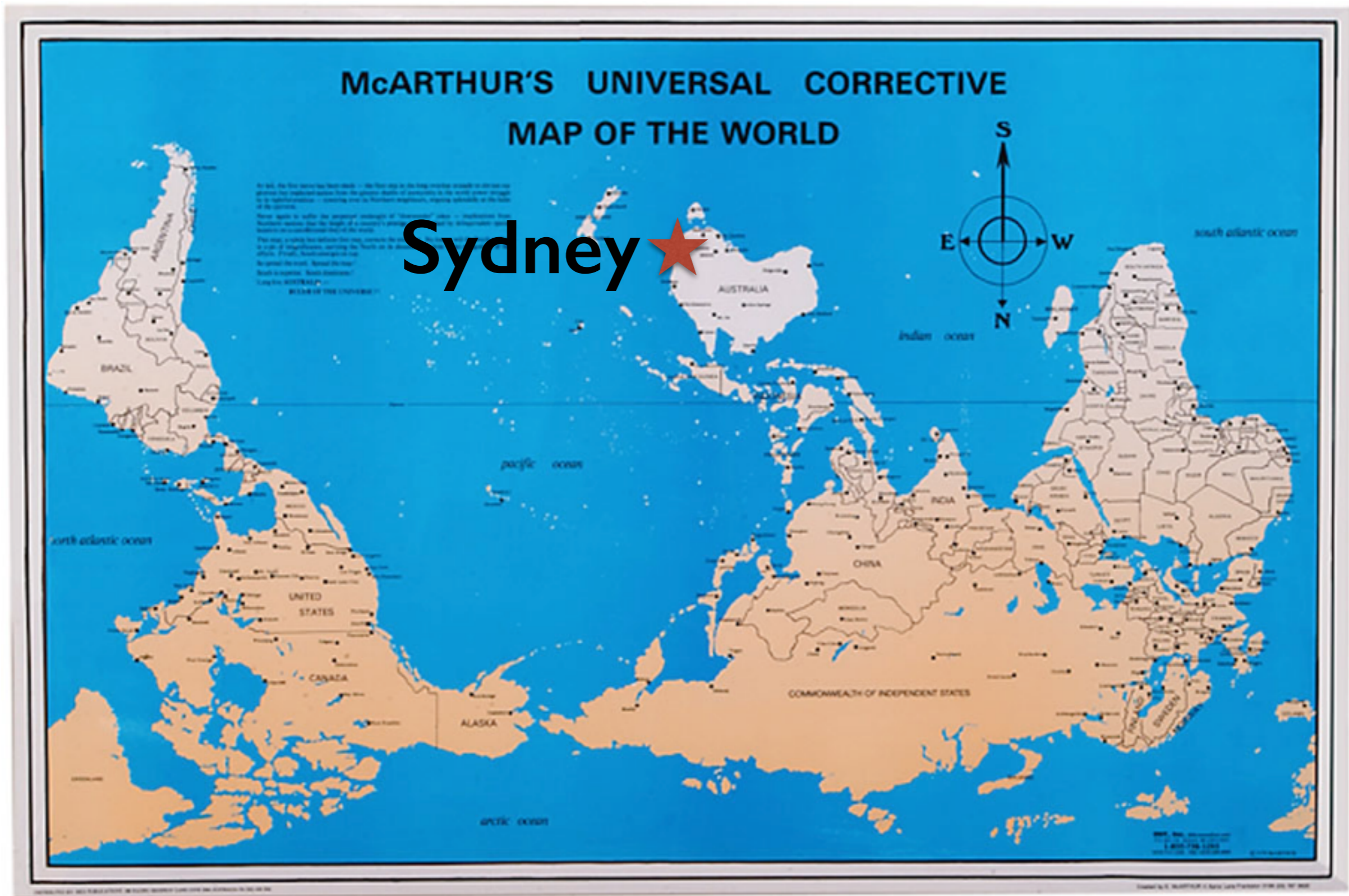
What is happening?

- **Post-Katrina:**

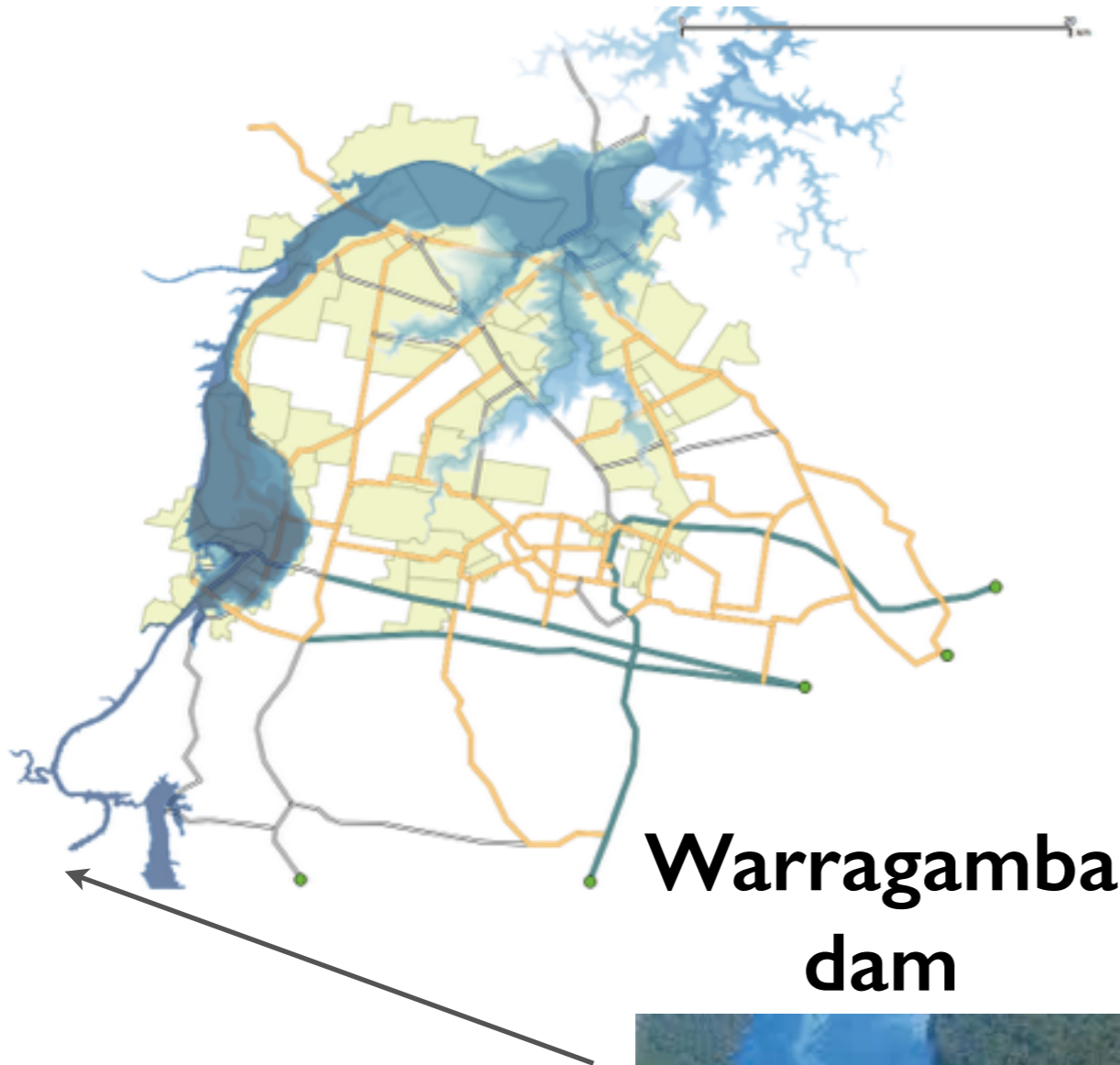
Need for advanced decision support

How can we mitigate negative effects and use resources more effectively?

Motivation



Motivation



Warragamba dam



smh.com.au
The Sydney Morning Herald

Environment

Weather Climate Change Whale Watch Animals Conservation Water Issues Energy Smart Ear

You are here: Home > Environment > Water Issues > Article

Urgent flood prevention measures needed for Warragamba Dam

November 3, 2012 ☆ Read later

Tim Barlass

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A one-in-1000 flood around the Hawkesbury Nepean, such as that in Queensland early last year, would cause up to \$8 billion in total damages affecting 14,000 homes and requires urgent preventative measures, according to a group of 10 western Sydney councils.

A one in 1000 flood is one that has a 0.1 per cent chance of happening each year.

The Western Sydney Regional Organisation of Councils last night called on the state government urgently to address threats of potential floods around the Hawkesbury Nepean.

A repeat of the 1867 flood would cause up to \$1.7 billion in direct damages and \$3 billion in total damages, the group said.

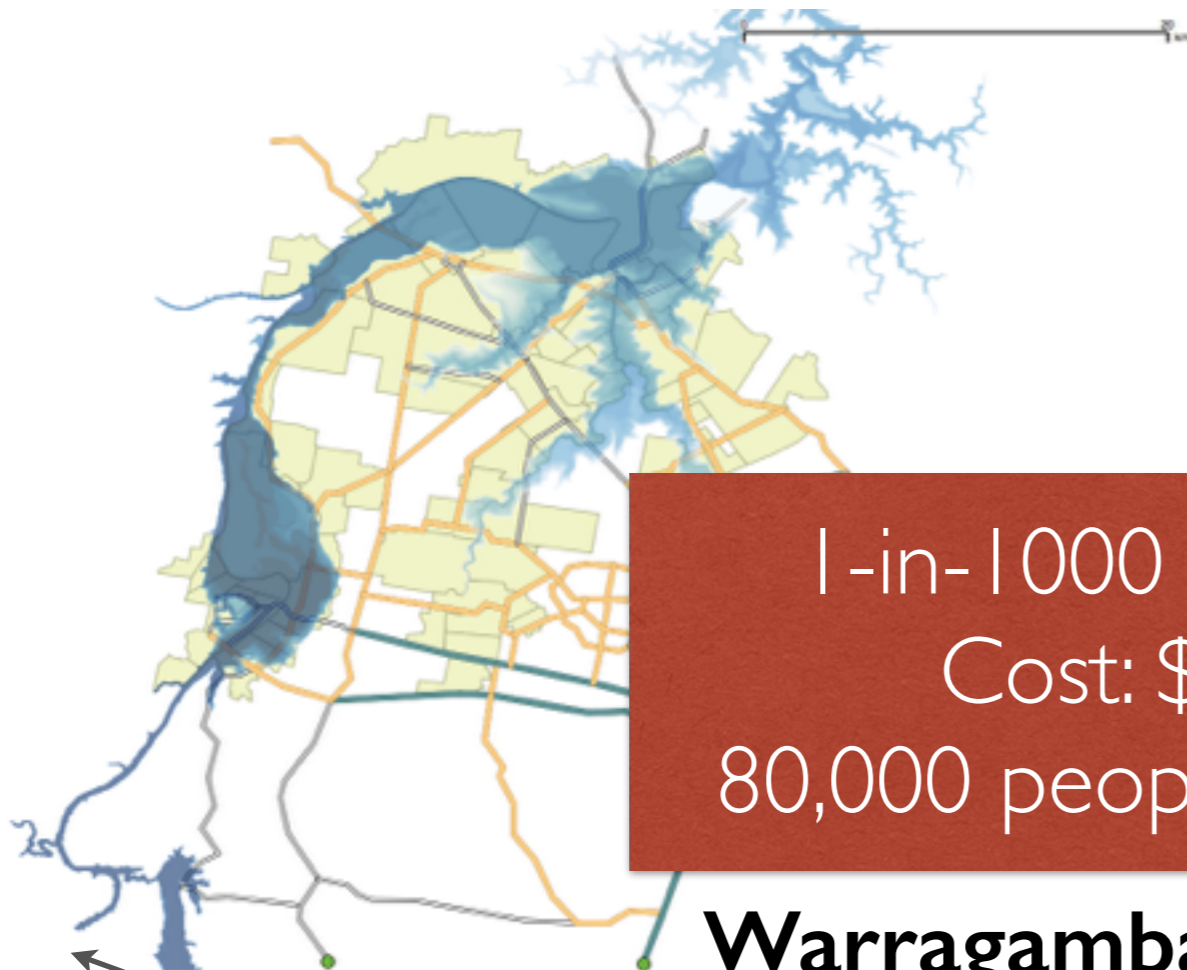
"This would affect an estimated 7600 homes, with about 1200 of those destroyed, WSROC president Tony Hadchiti said.

Flood prevention measures could include raising the wall of the Warragamba Dam, which filled to capacity in March, spilling water over the wall.

Infrastructure NSW last month backed the implementation of Hawkesbury Nepean Flood Plain mitigation measures as a key recommendation of its 20-year strategy "First Things First".

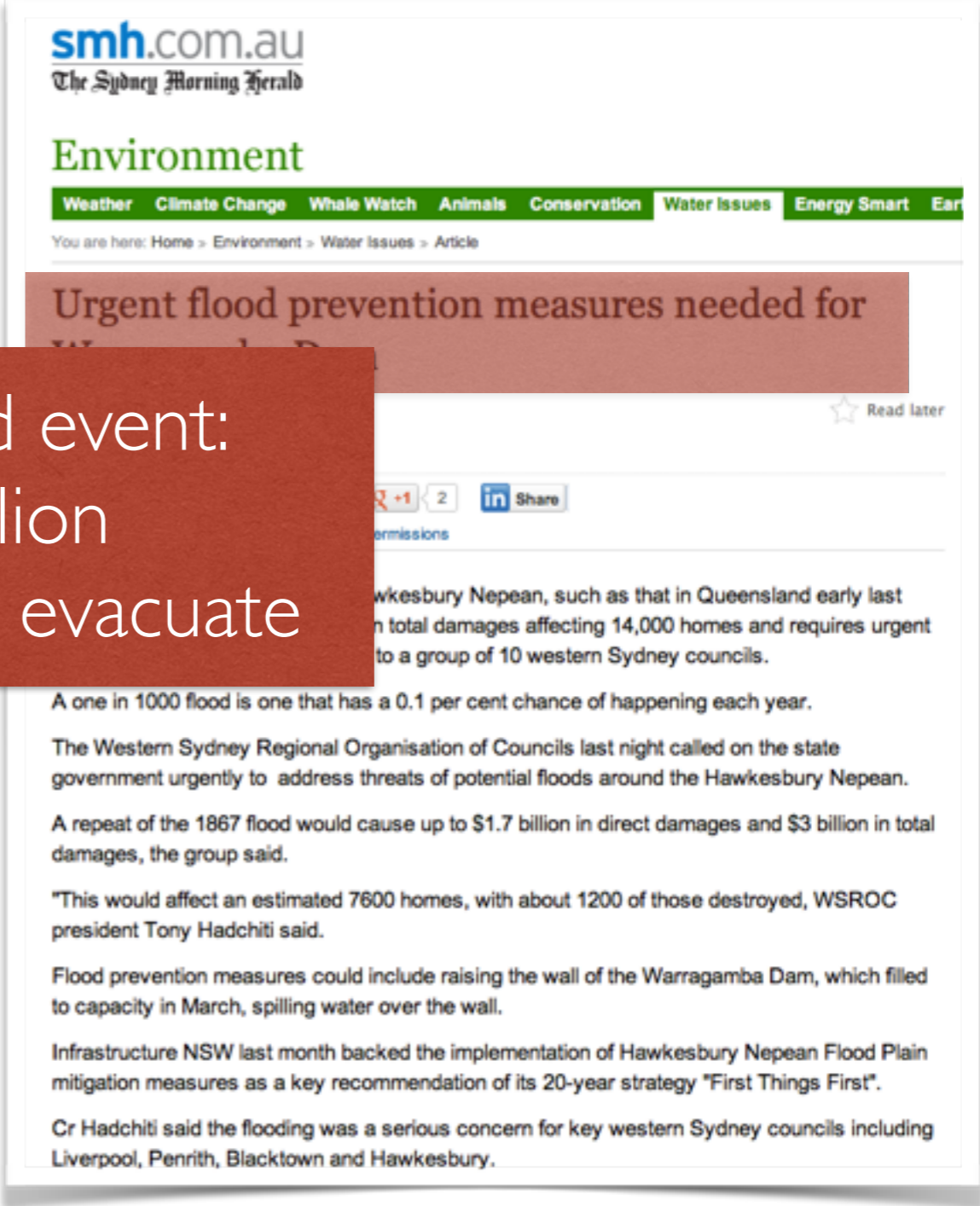
Cr Hadchiti said the flooding was a serious concern for key western Sydney councils including Liverpool, Penrith, Blacktown and Hawkesbury.

Motivation



1-in-1000 flood event:
Cost: \$8 billion
80,000 people to evacuate

Warragamba dam



The screenshot shows a news article from the Sydney Morning Herald (smh.com.au) under the 'Environment' section. The article title is 'Urgent flood prevention measures needed for Hawkesbury Nepean'. The article discusses the need for urgent action to address flood threats in the region, citing a 1-in-1000 flood event with a 0.1% chance of occurring each year. It mentions that a repeat of the 1867 flood would cause significant damage and that Infrastructure NSW has backed flood plain mitigation measures. The article also notes that the Warragamba Dam was filled to capacity in March, spilling water over the wall.

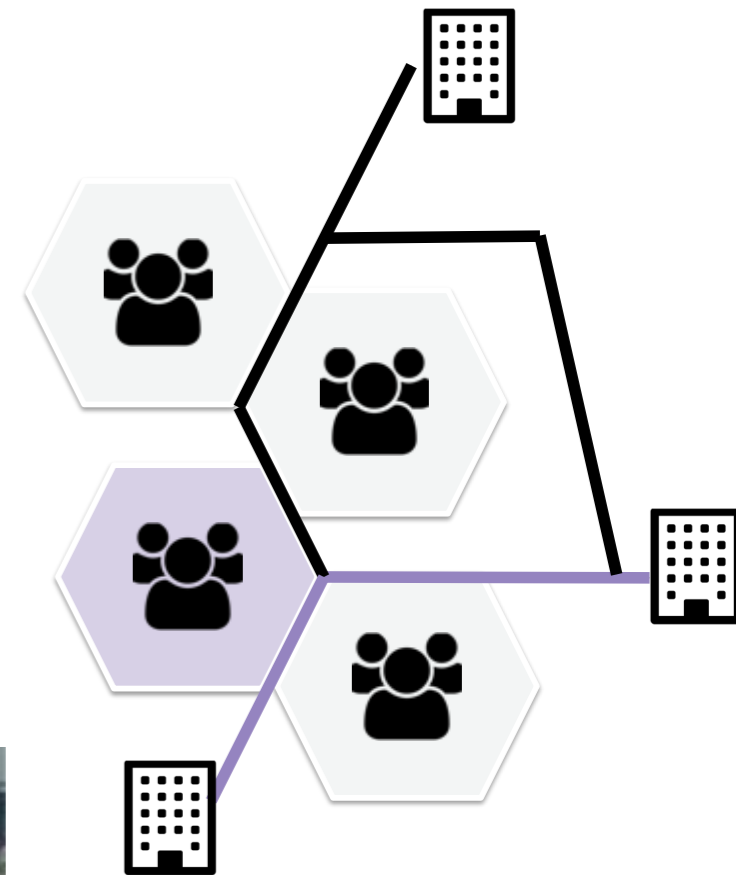
Evacuation planning

- **Decisions**

- When to evacuate
- Where to go?
- Which route to follow?

- **Constraints**

- Avoid congestion
- Ensure safety of evacuees

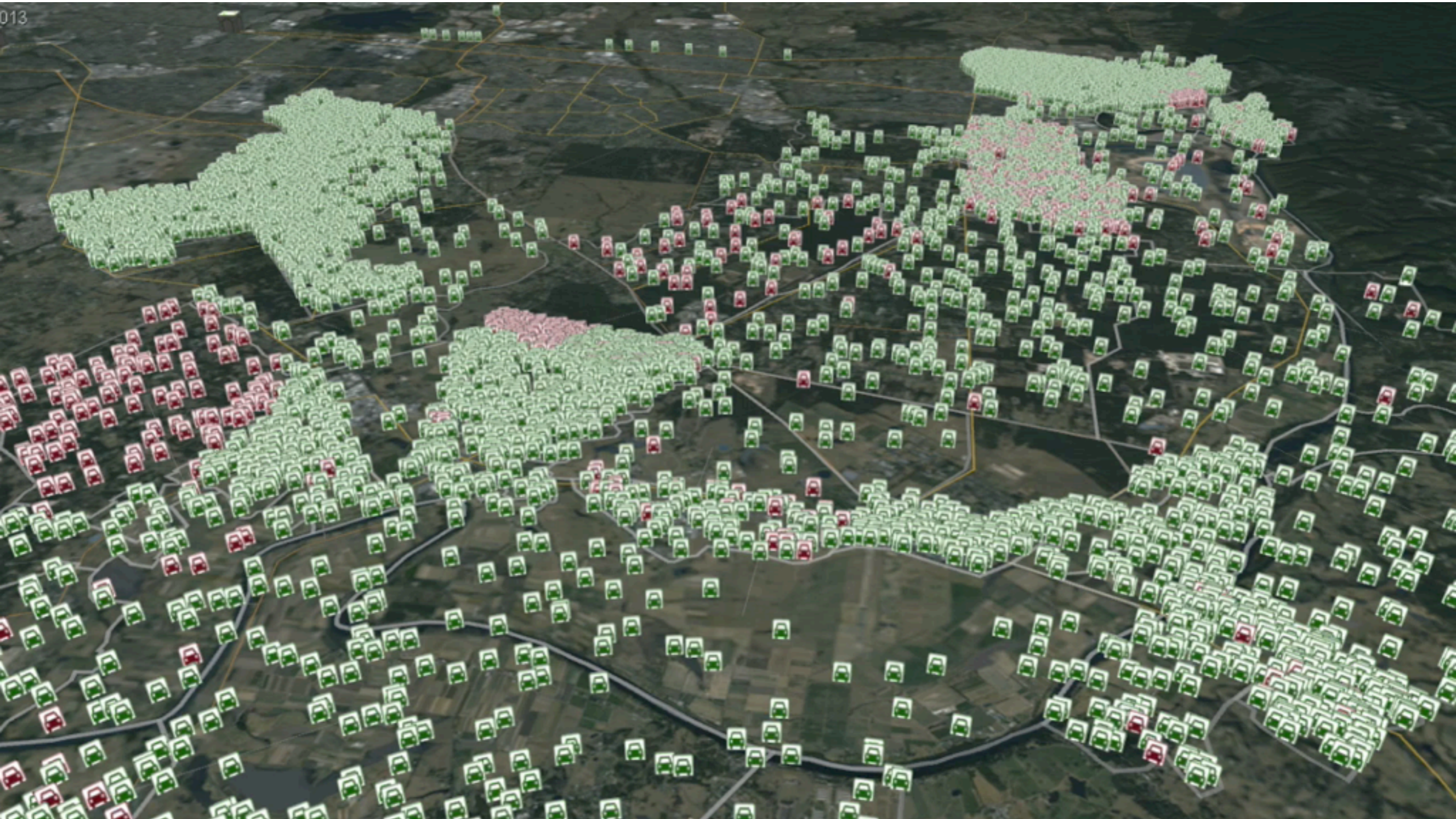


Evacuation planning

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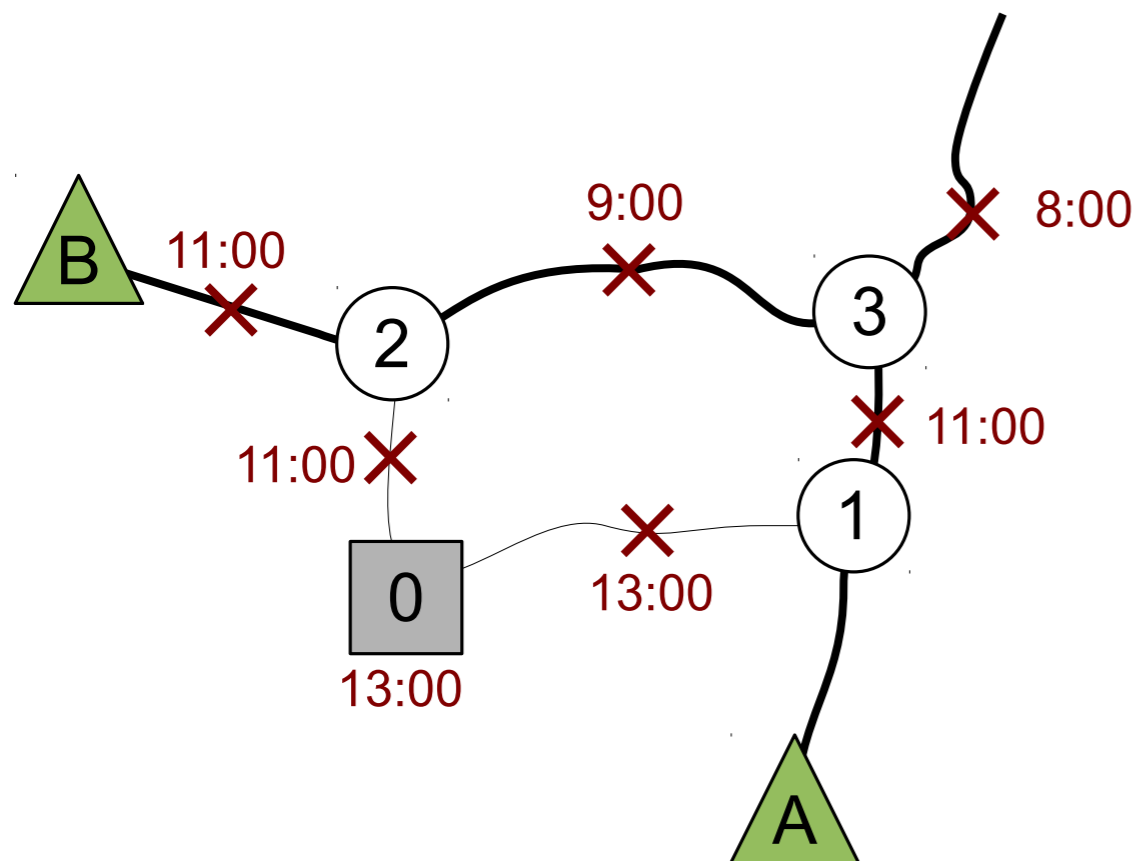
Evacuation of 80,000 persons



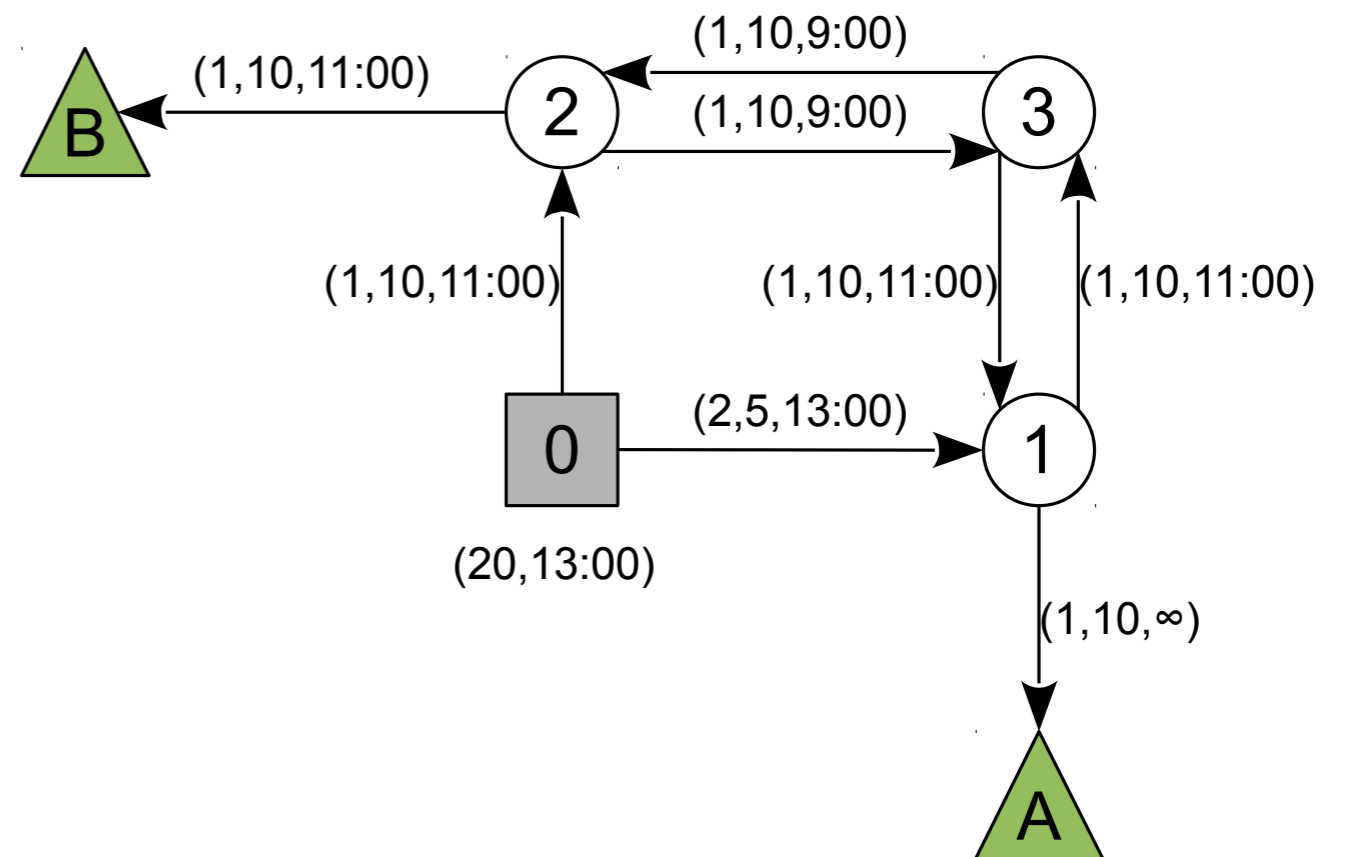
Evacuation of 80,000 persons



Evacuation Scenario

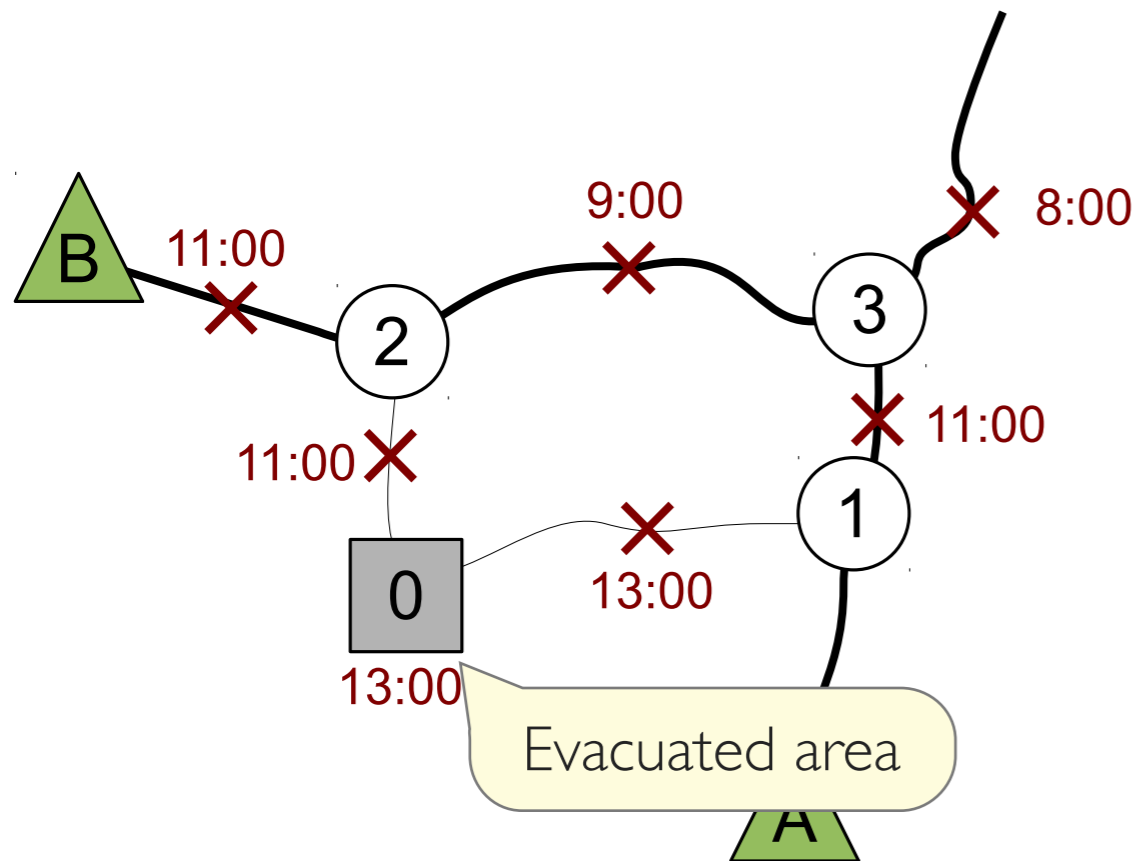


Real-world scenario

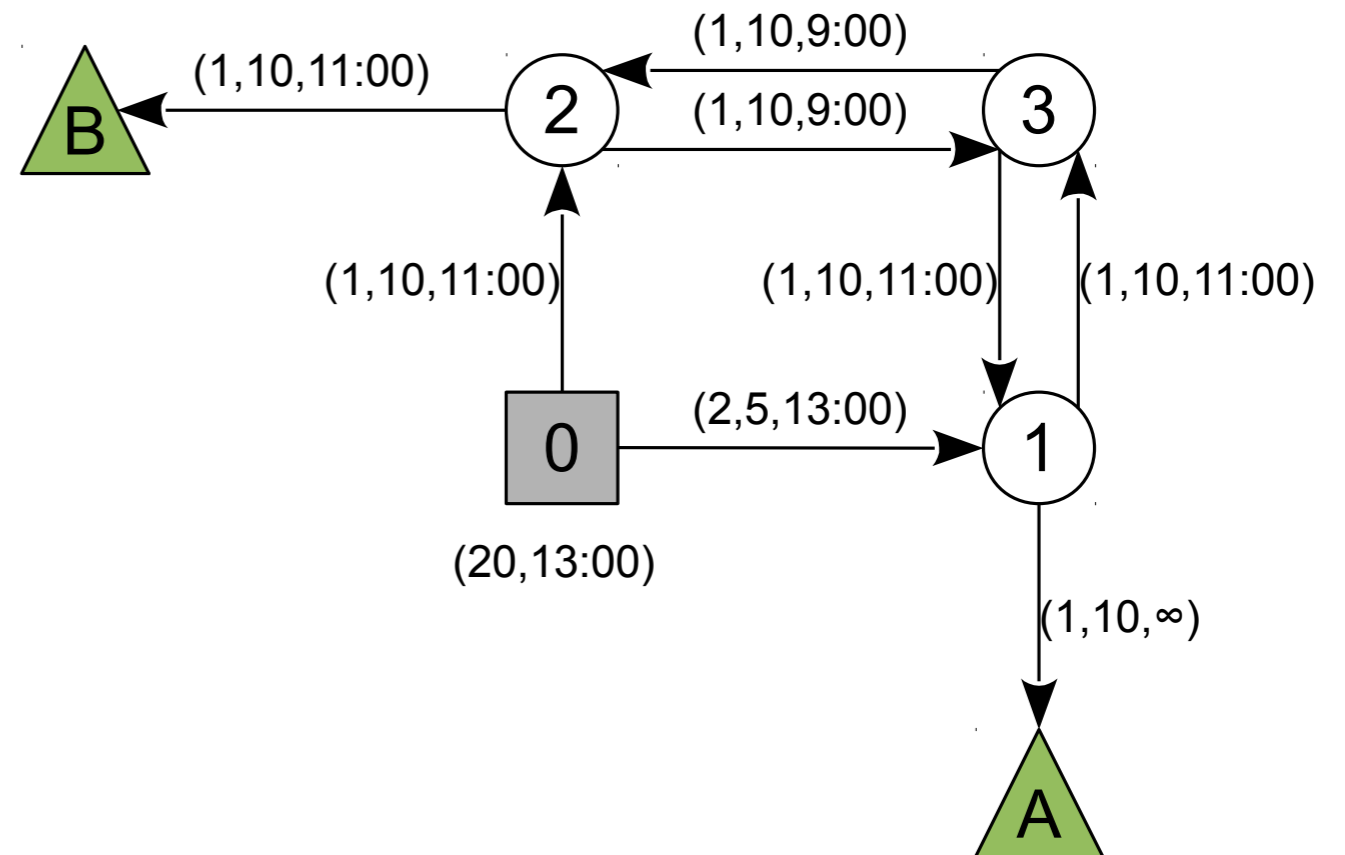


Evacuation graph

Evacuation Scenario

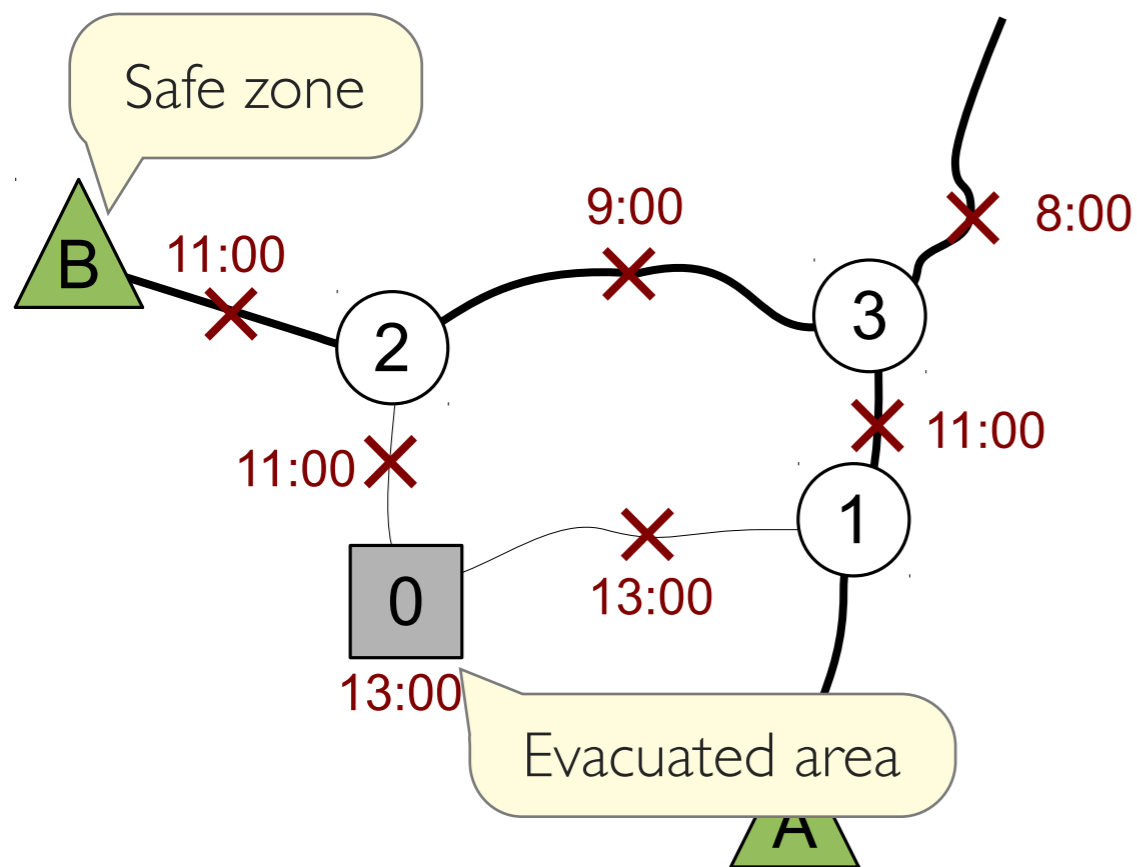


Real-world scenario

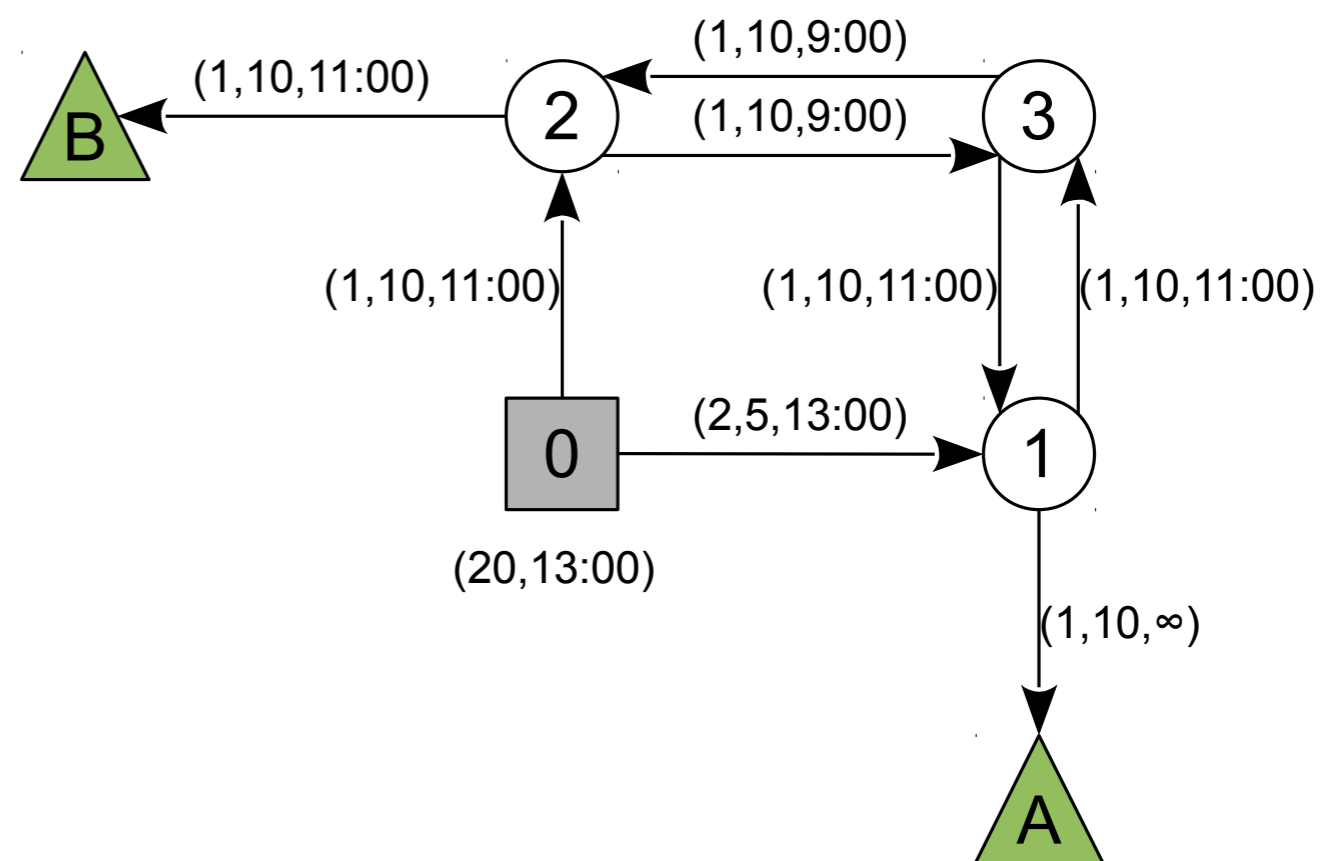


Evacuation graph

Evacuation Scenario

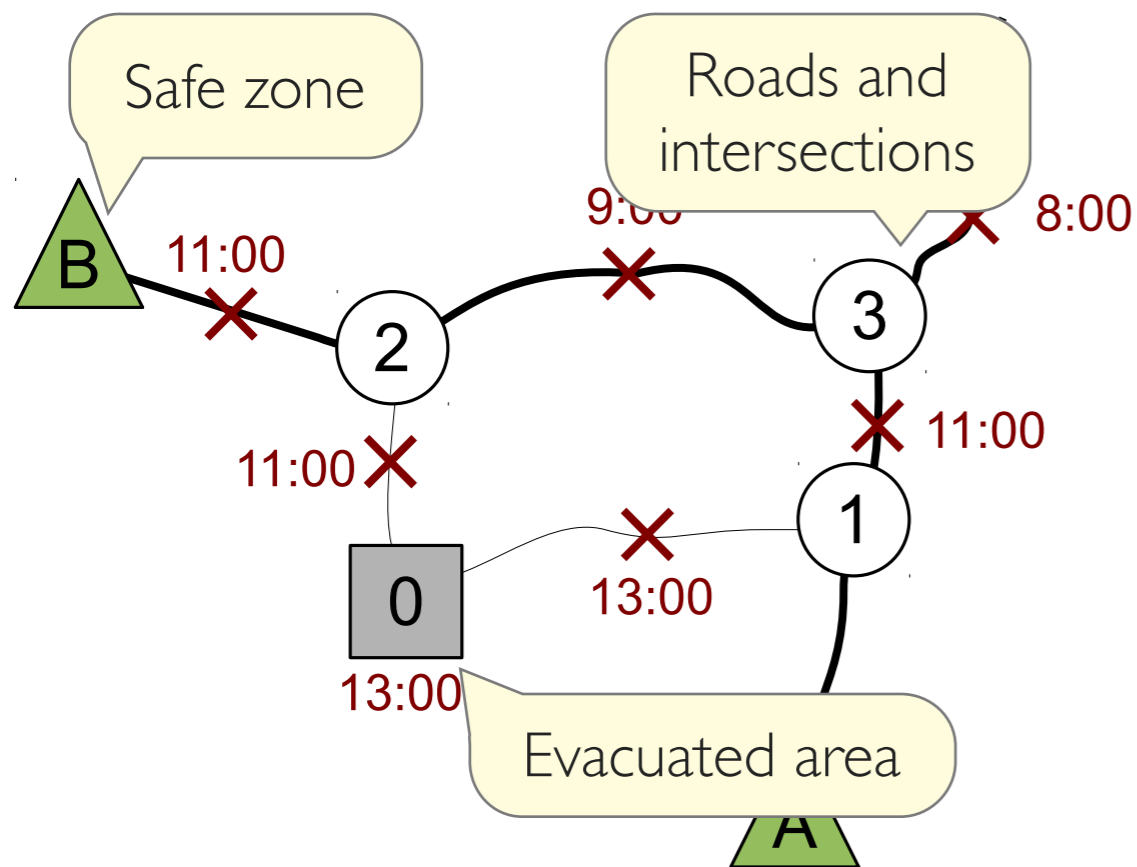


Real-world scenario

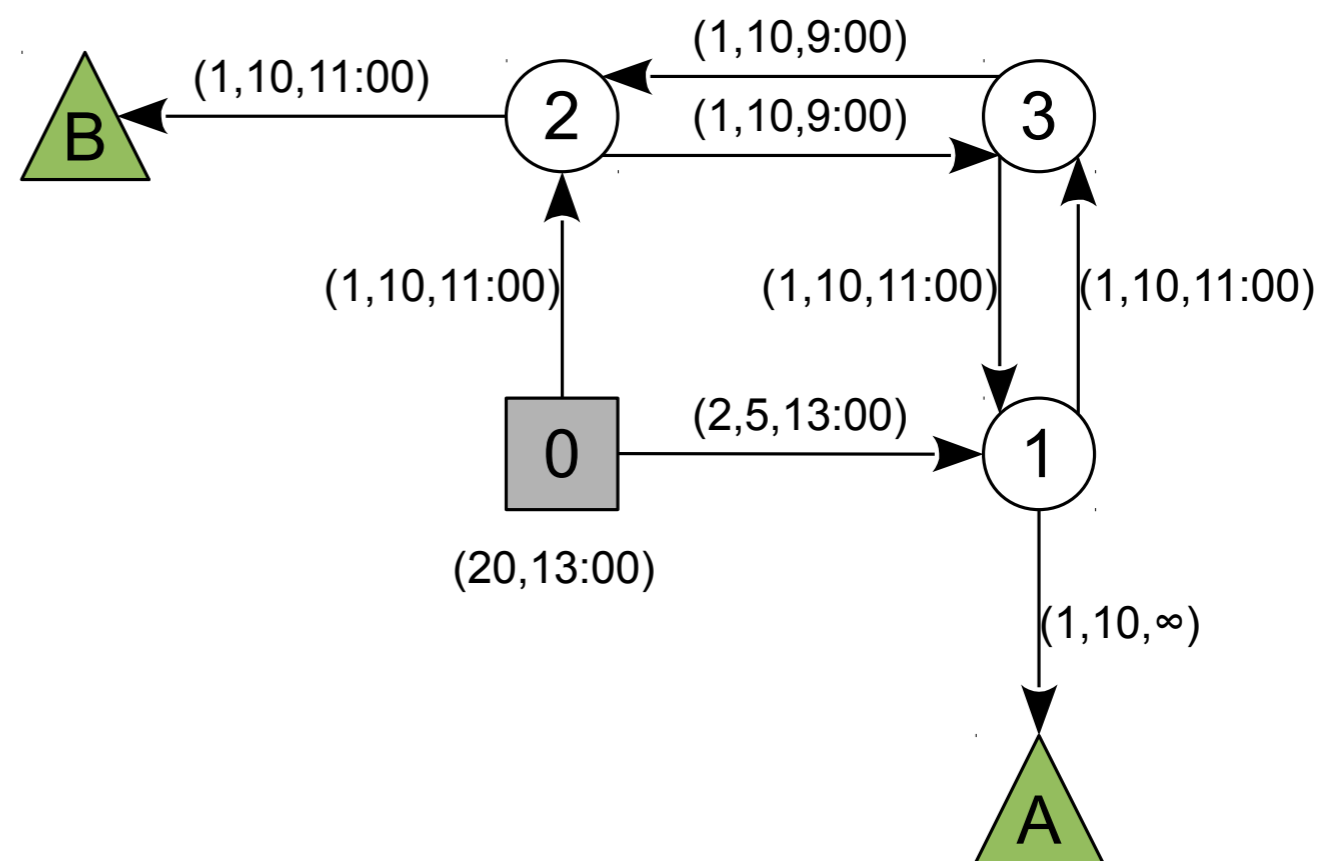


Evacuation graph

Evacuation Scenario

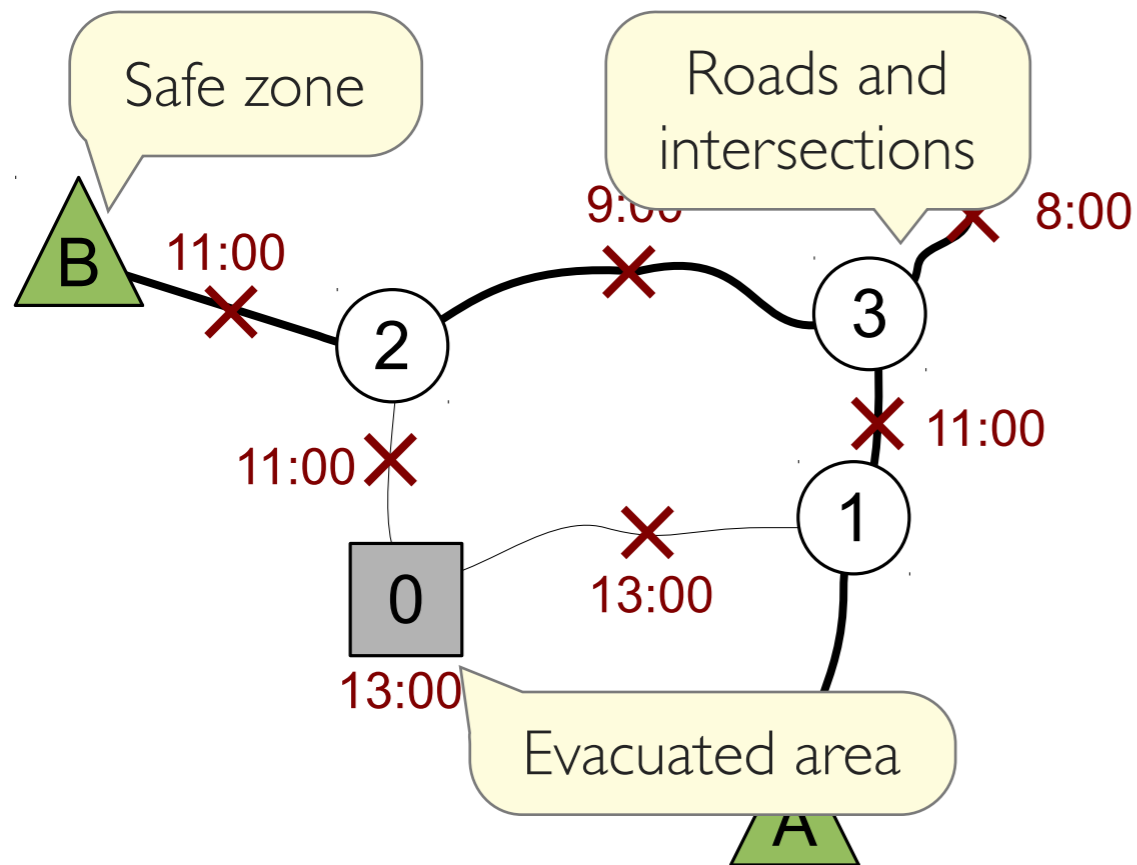


Real-world scenario

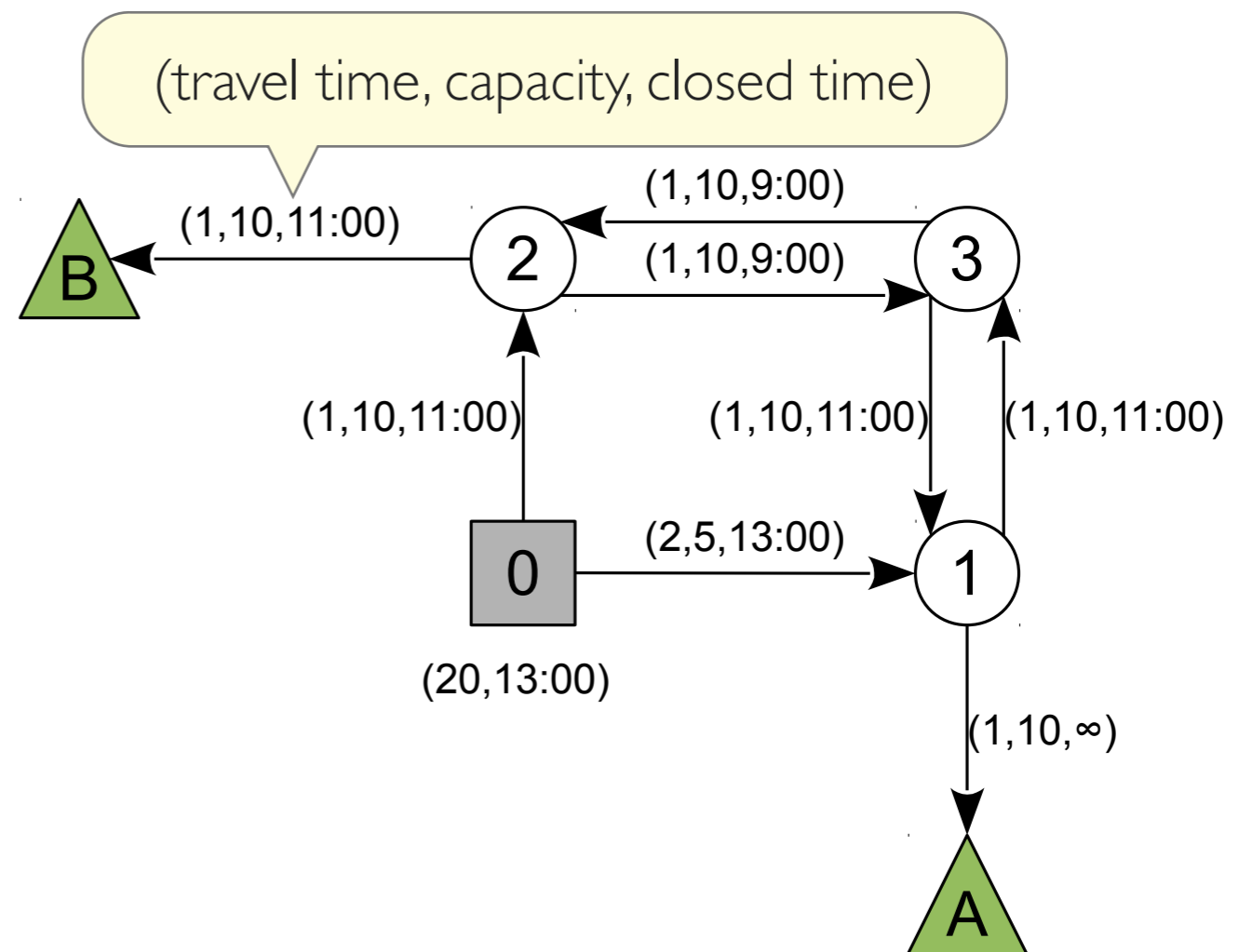


Evacuation graph

Evacuation Scenario

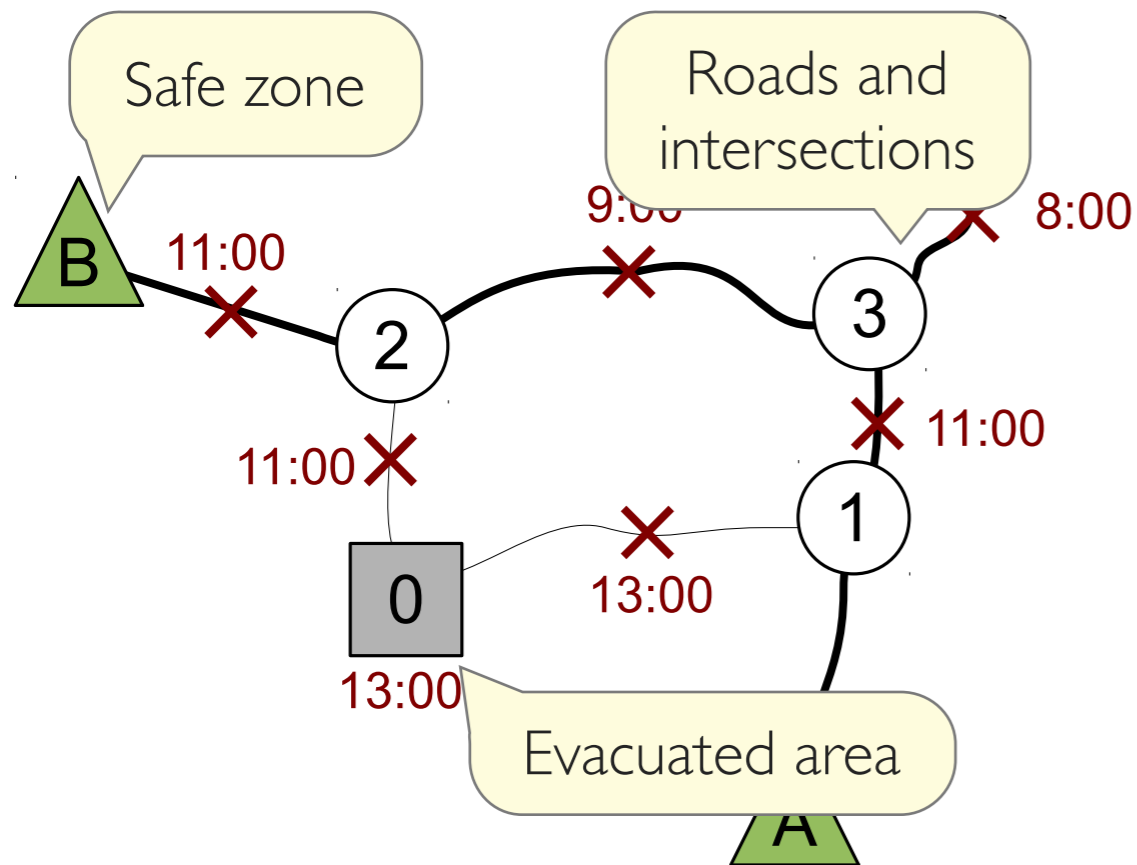


Real-world scenario

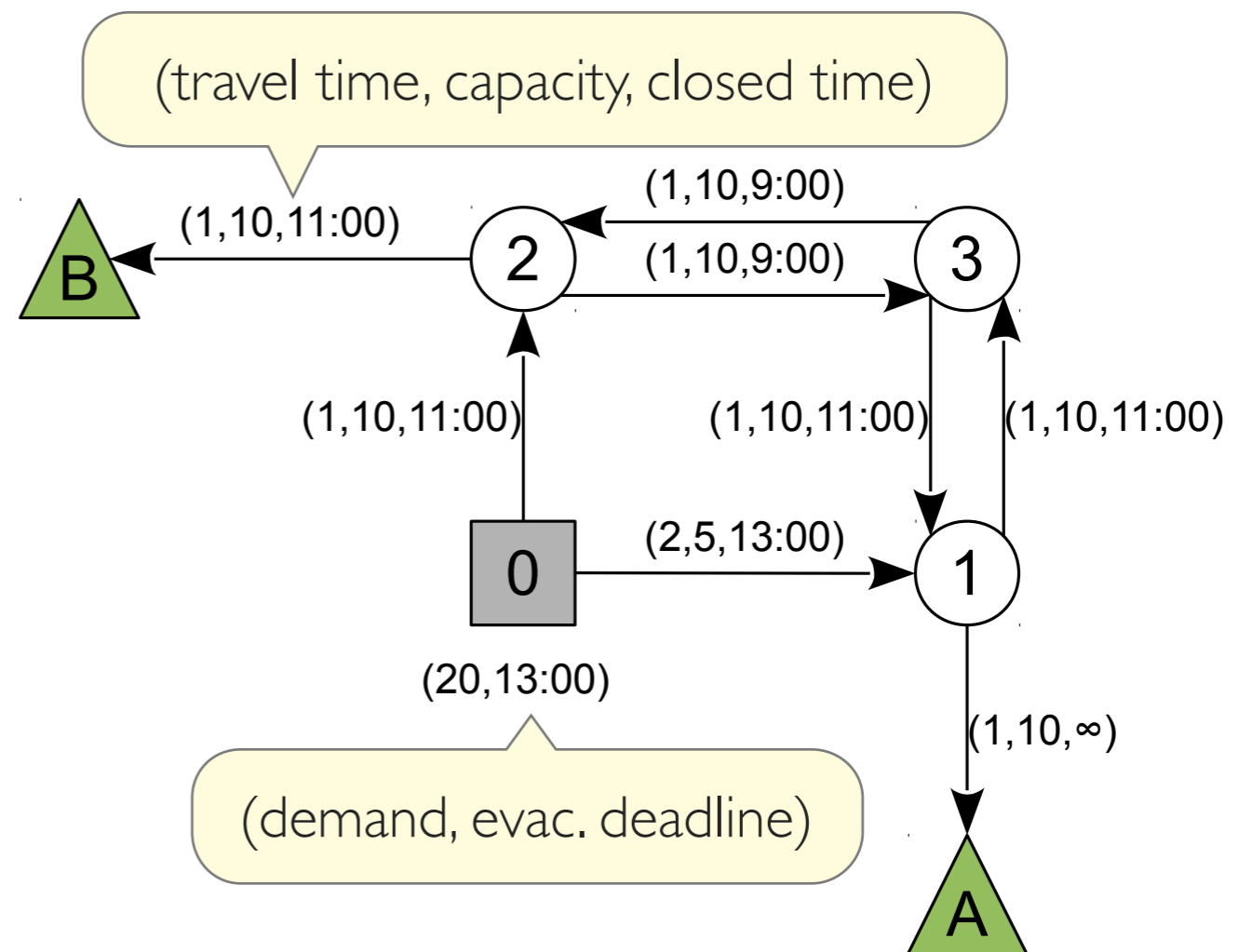


Evacuation graph

Evacuation Scenario

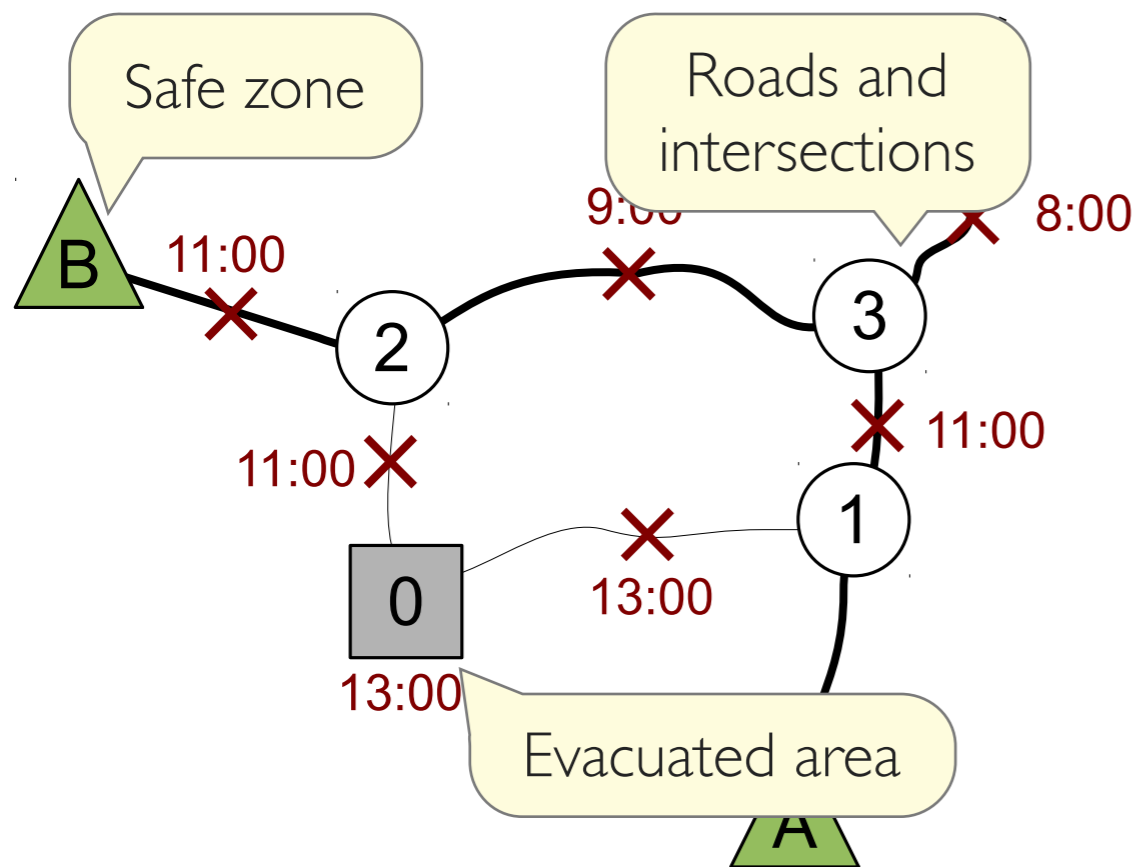


Real-world scenario

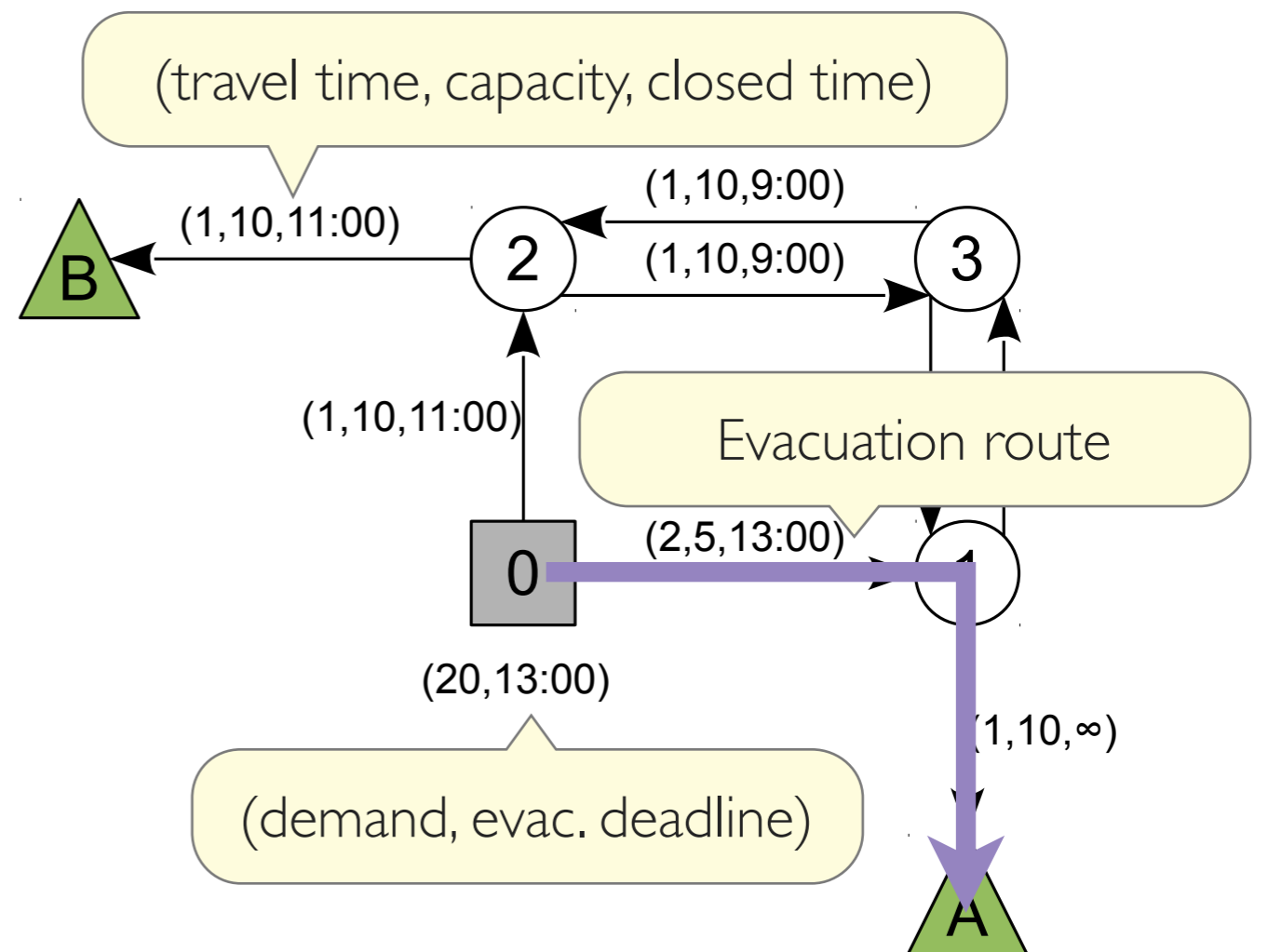


Evacuation graph

Evacuation Scenario



Real-world scenario



Evacuation graph

Contraflows

- Increase outbound capacity by changing lane direction
- In practice: highways and major roads



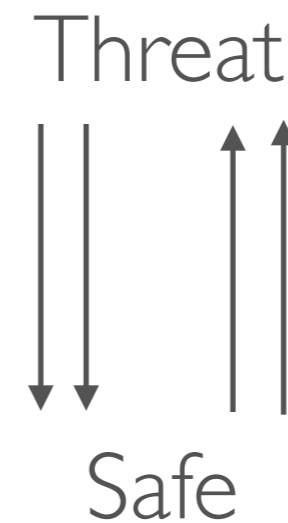
Houston, TX

Contraflows

- Increase outbound capacity by changing lane direction
- In practice: highways and major roads



Houston, TX

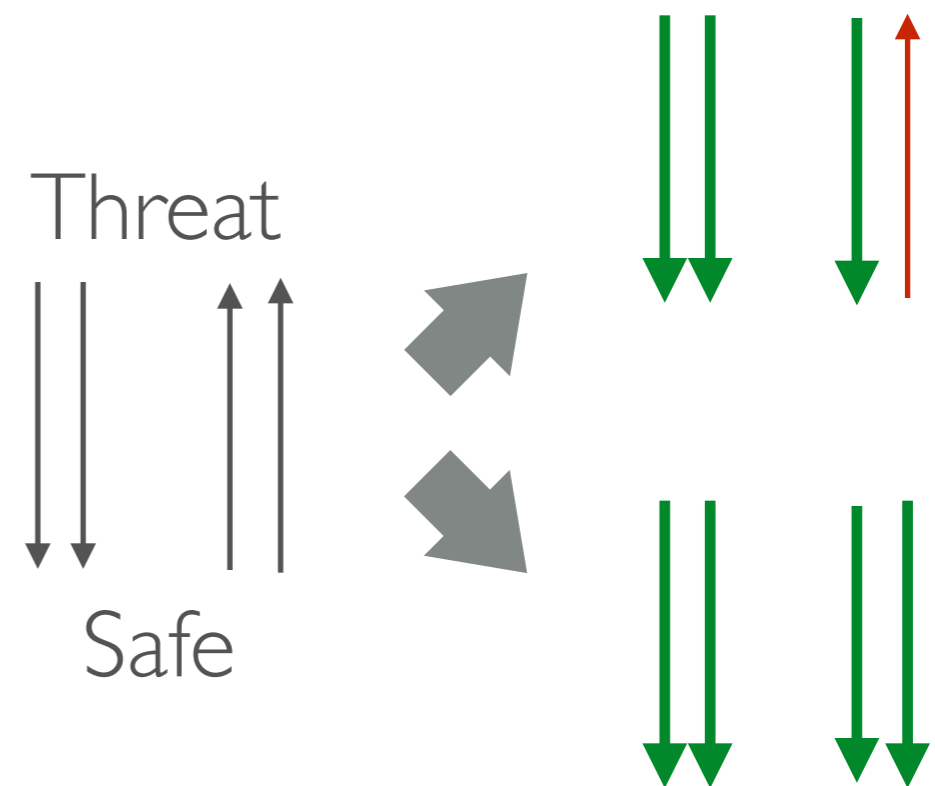


Contraflows

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- In practice: highways and major roads

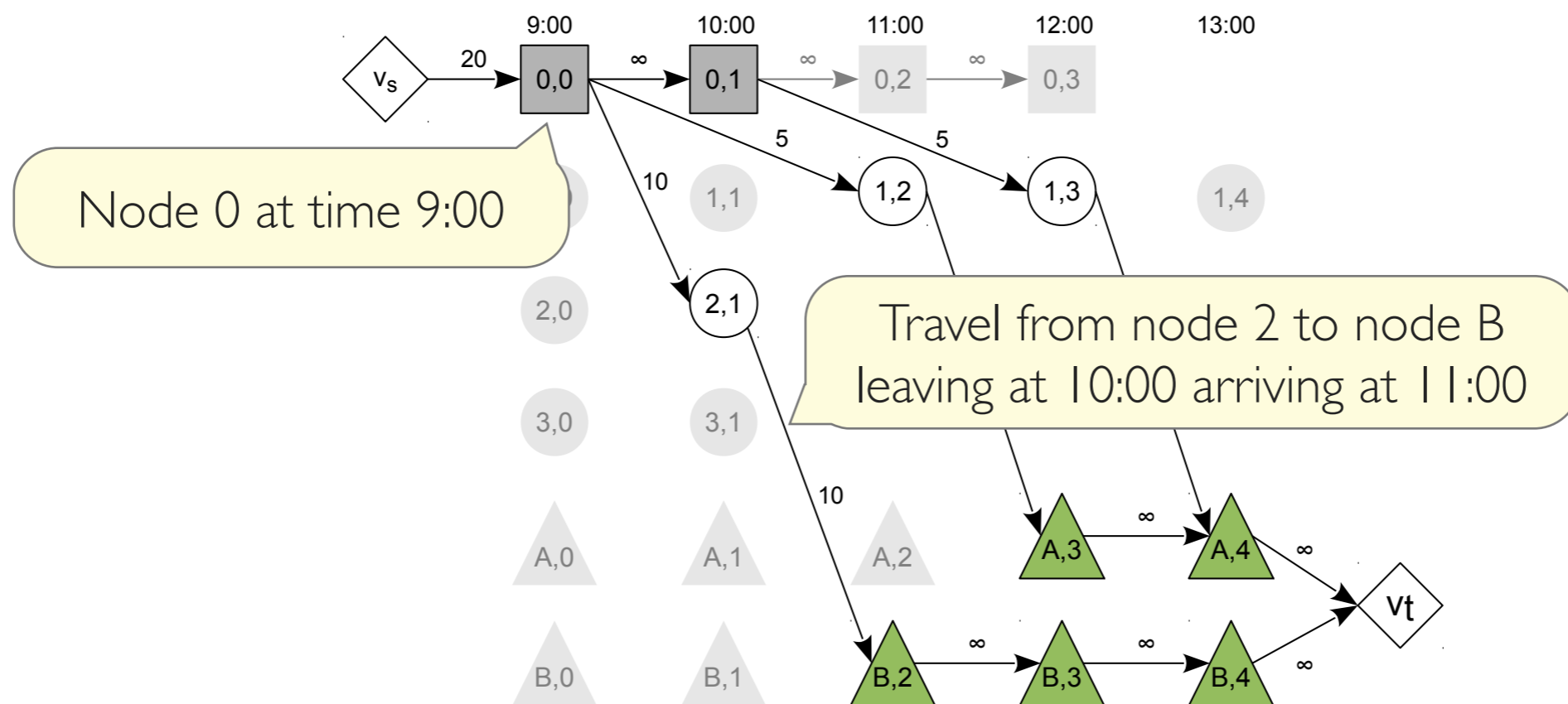


Houston, TX

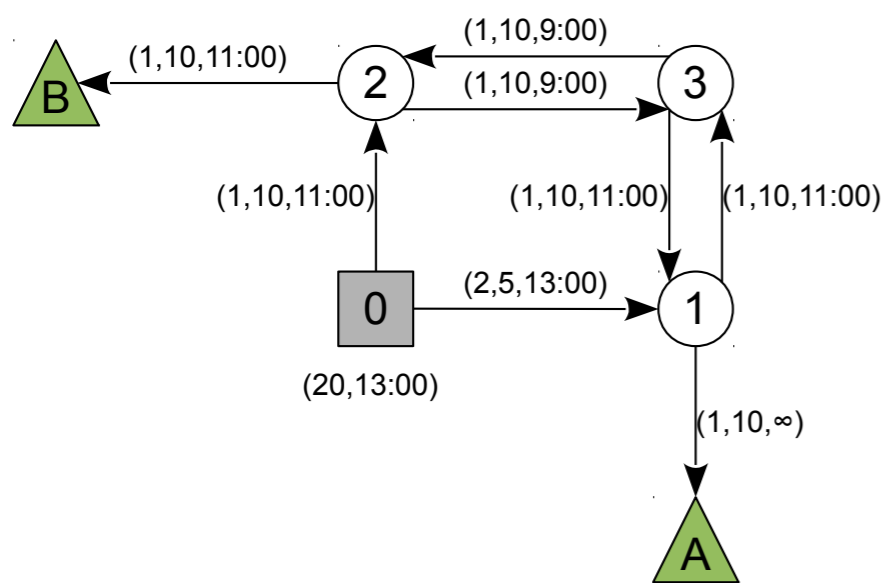


Evacuation Scheduling

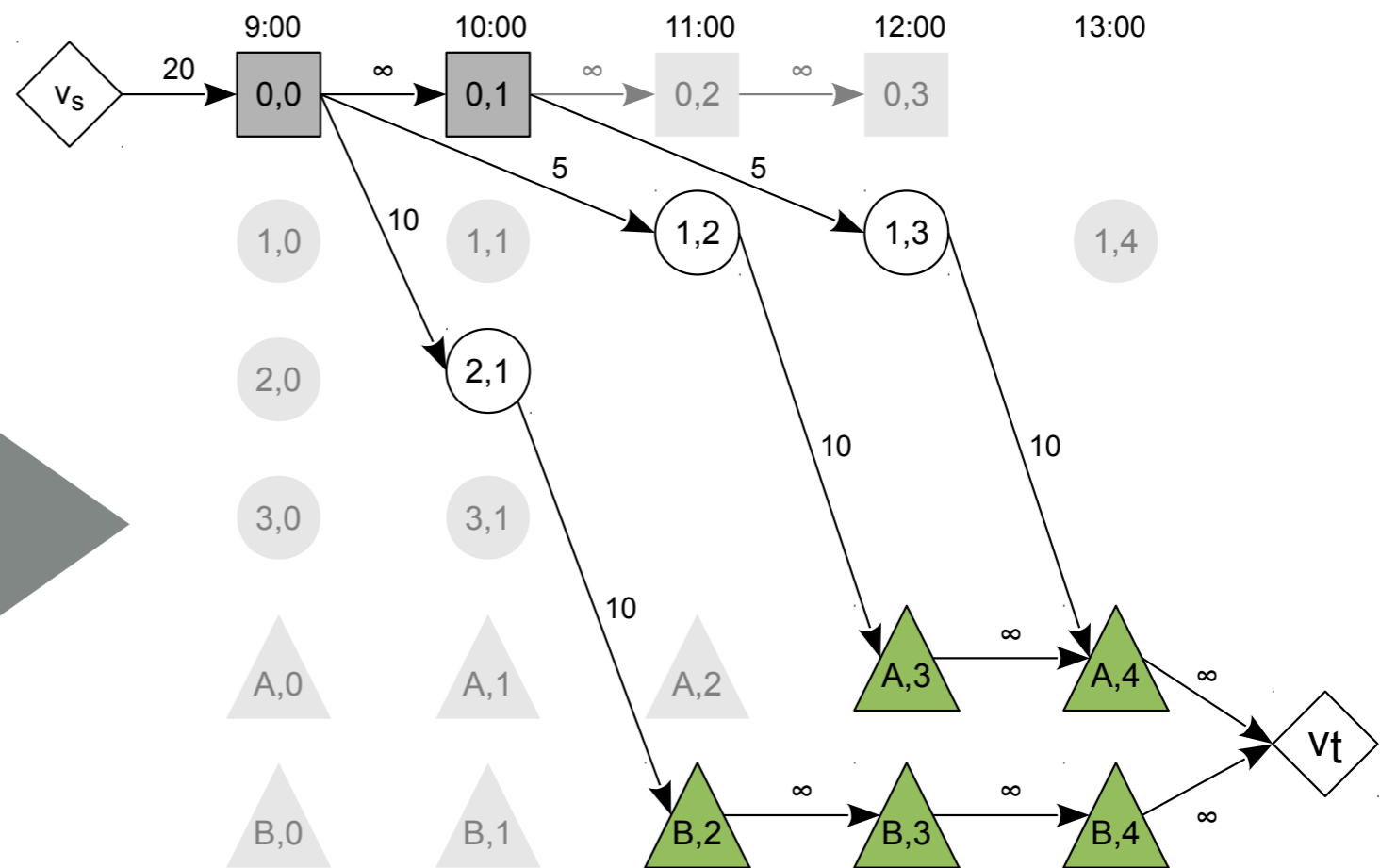
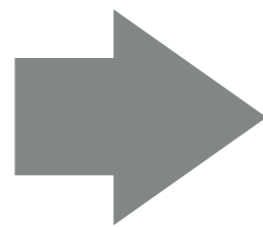
- The problem is to schedule the evacuation over time
 - Given evacuation routes
 - Decide when each evacuee leaves
- Modeled using a Time-Expanded Graph:



Evacuation Scheduling

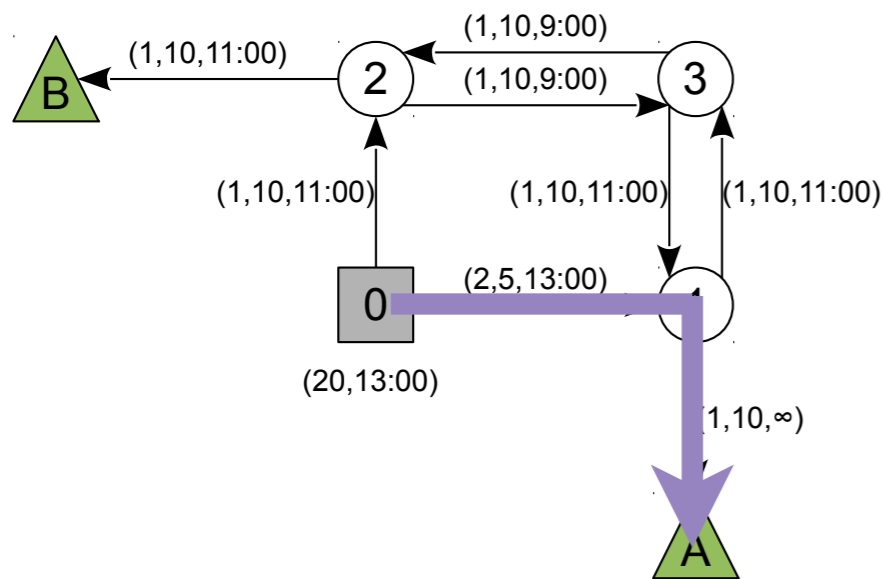


Evacuation route

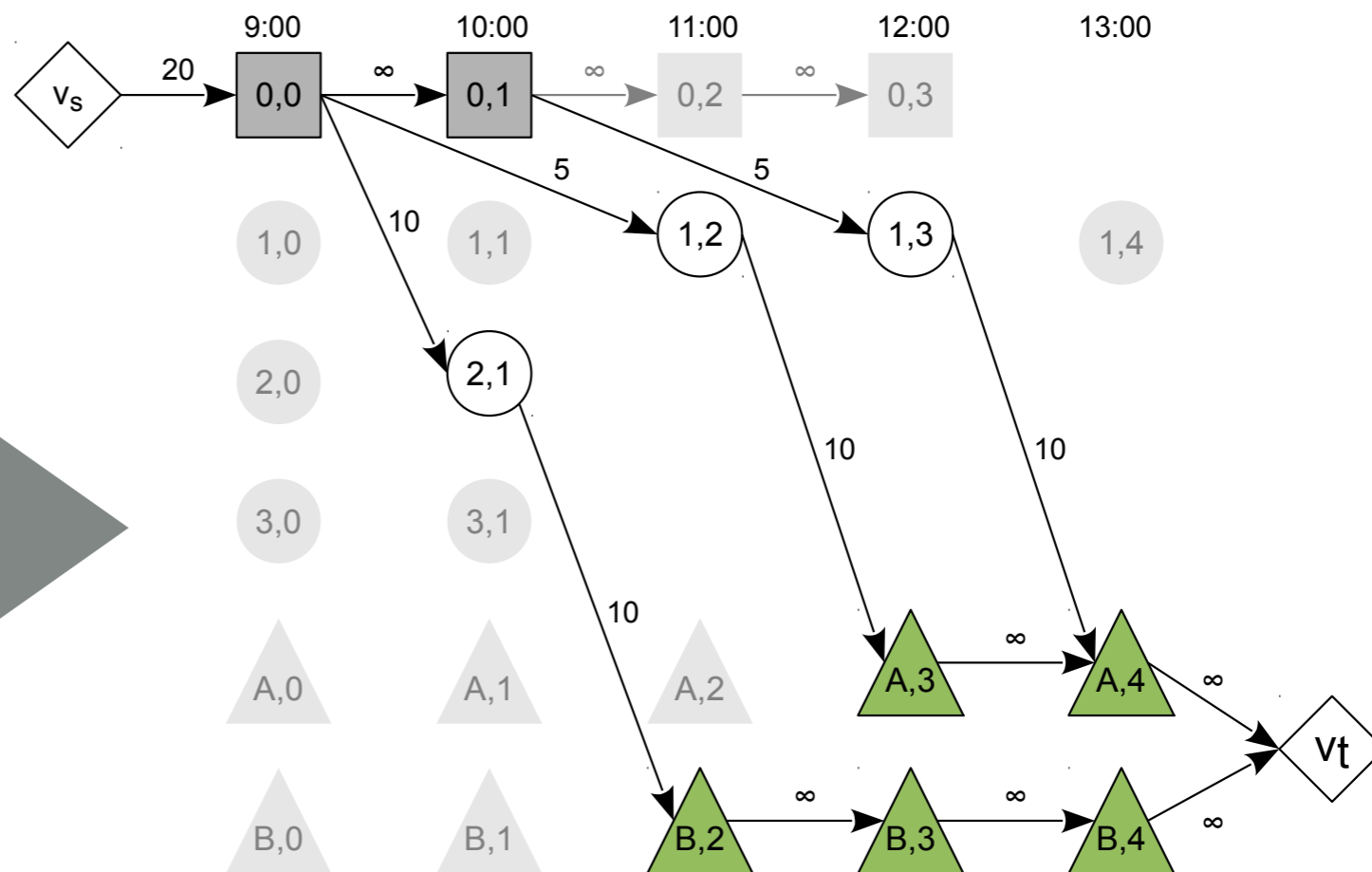
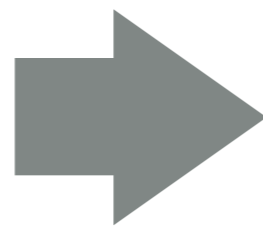


Evacuation schedule

Evacuation Scheduling



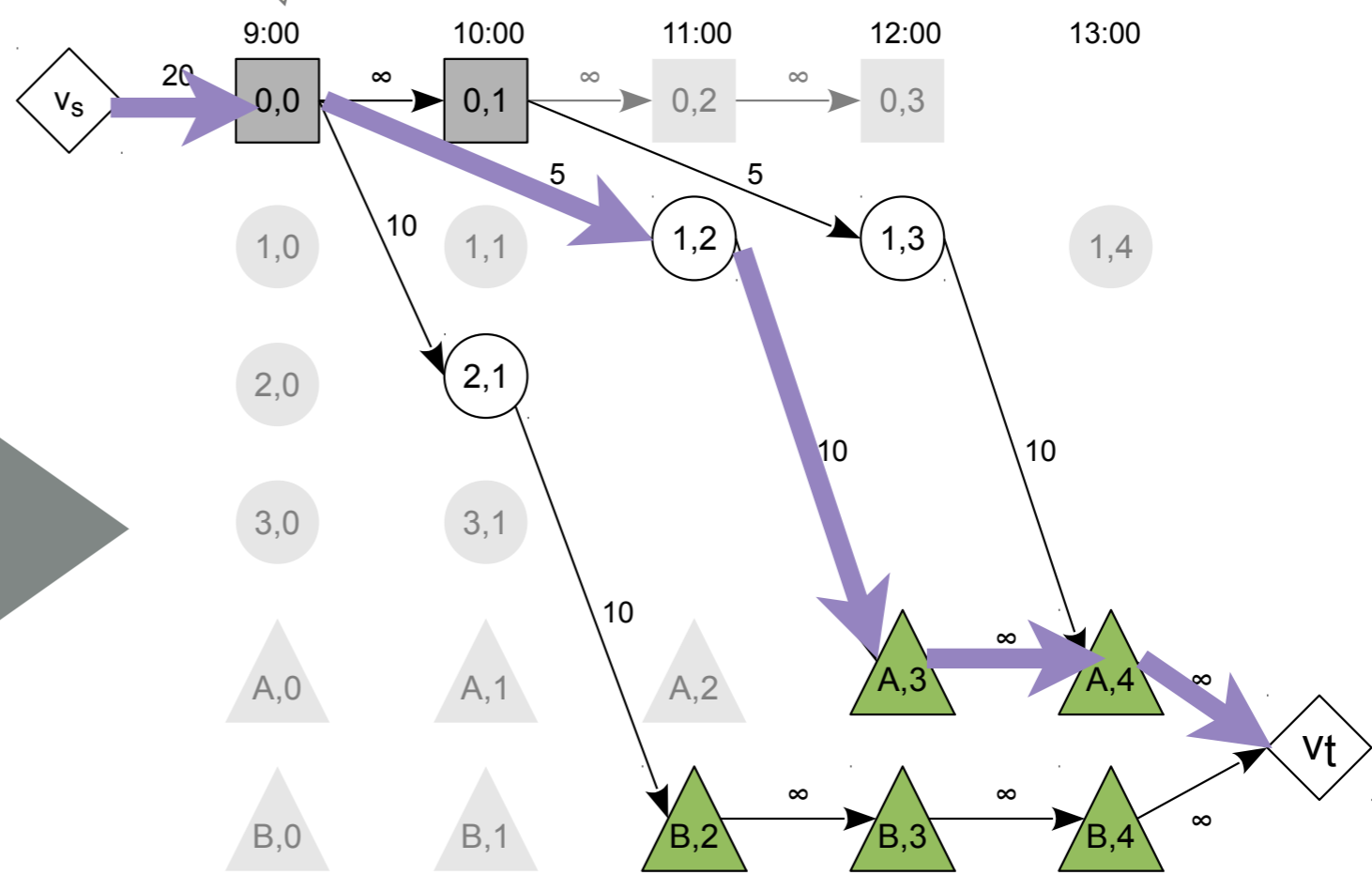
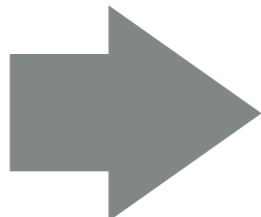
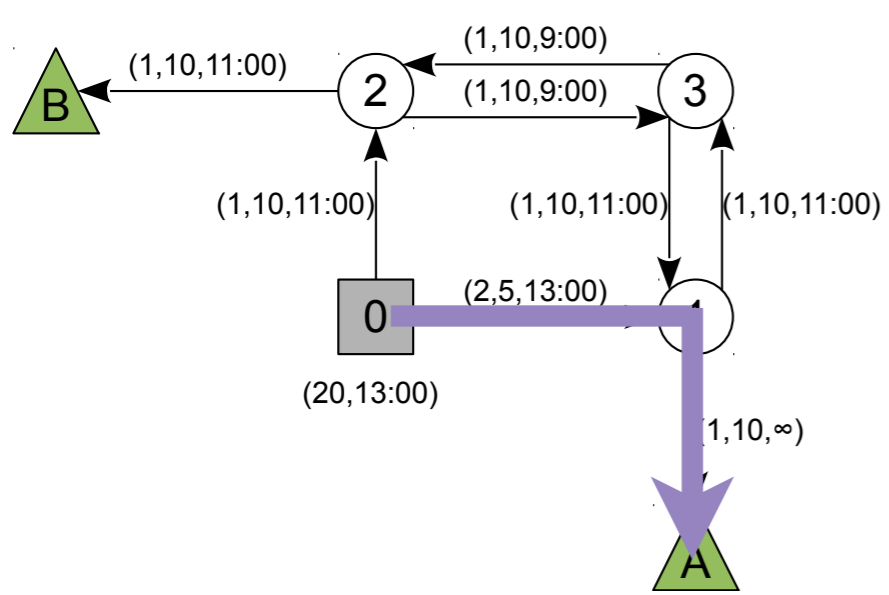
Evacuation route



Evacuation schedule

Evacuation Scheduling

5 leaving at 9:00



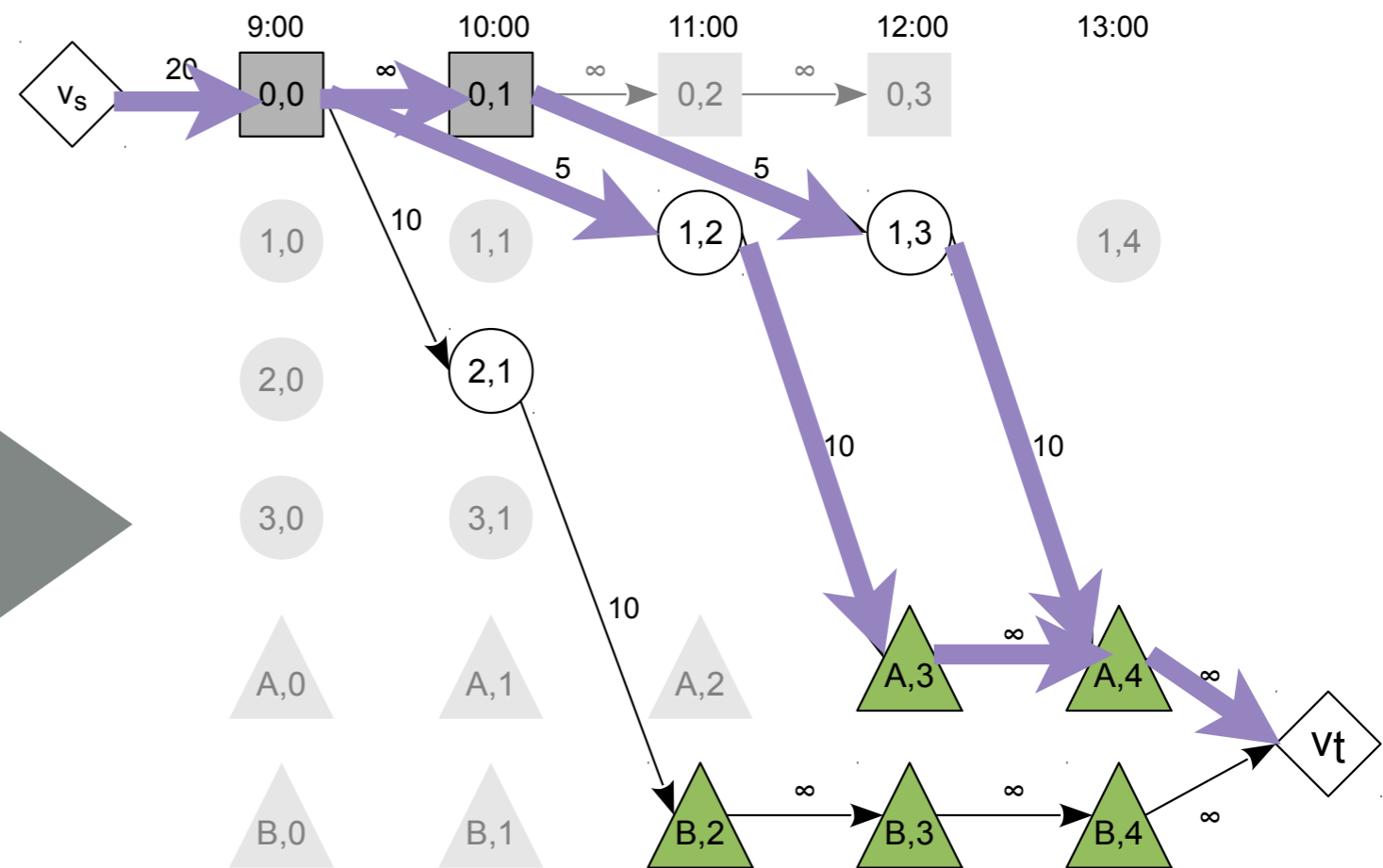
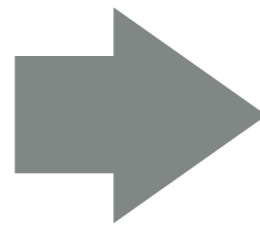
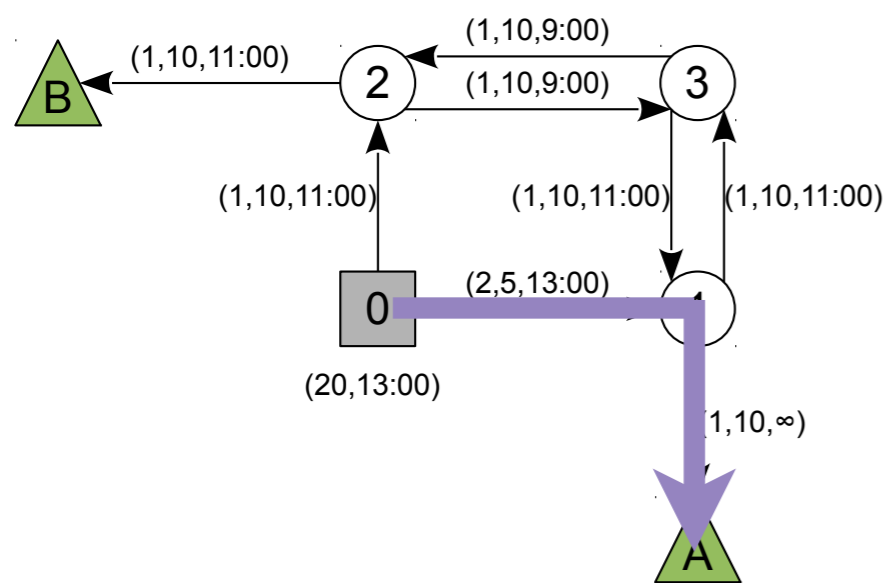
Evacuation route

Evacuation schedule

Evacuation Scheduling

5 leaving at 9:00

5 leaving at 10:00



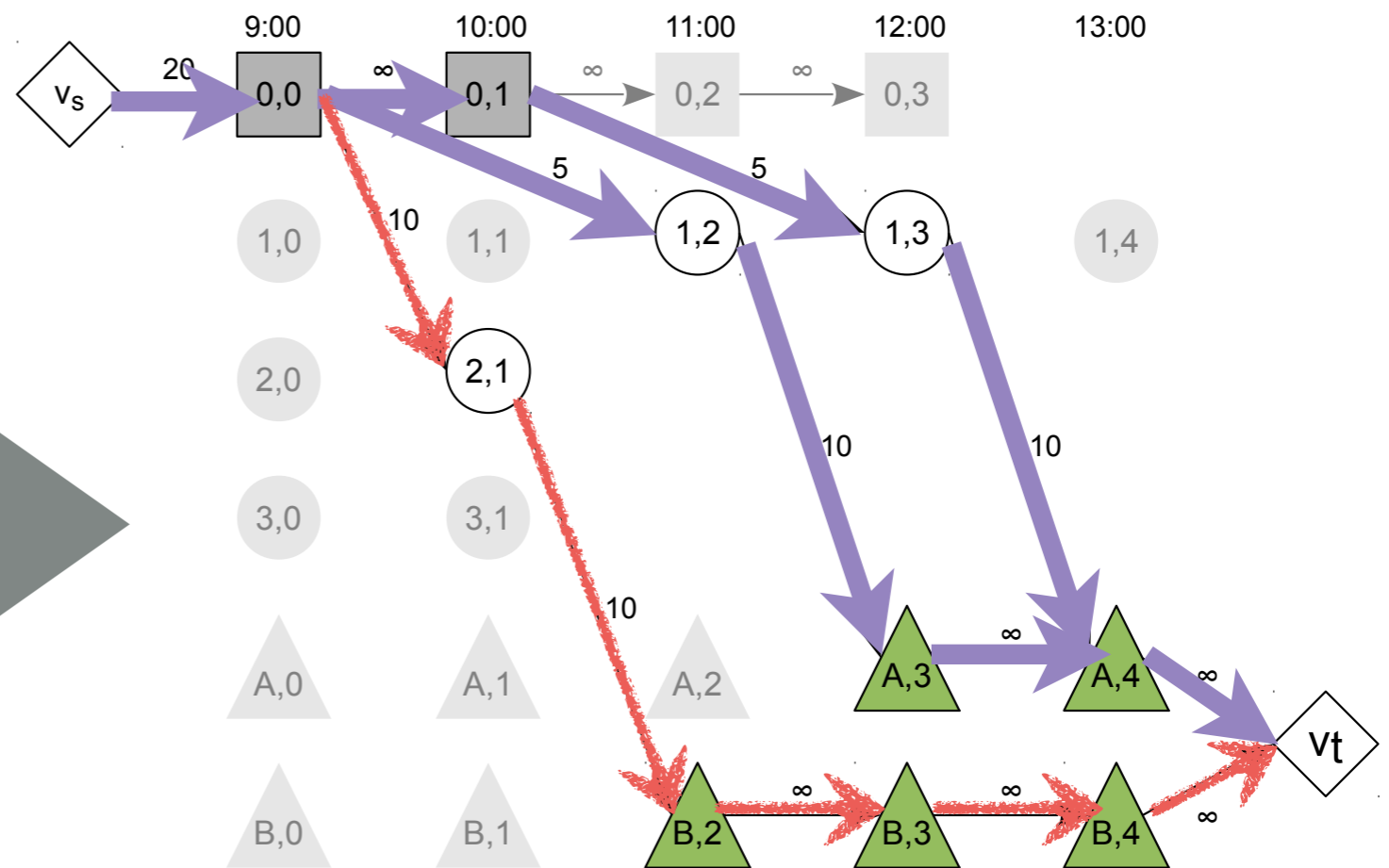
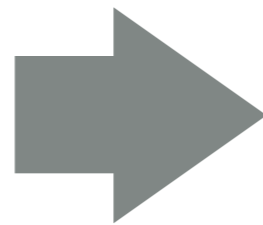
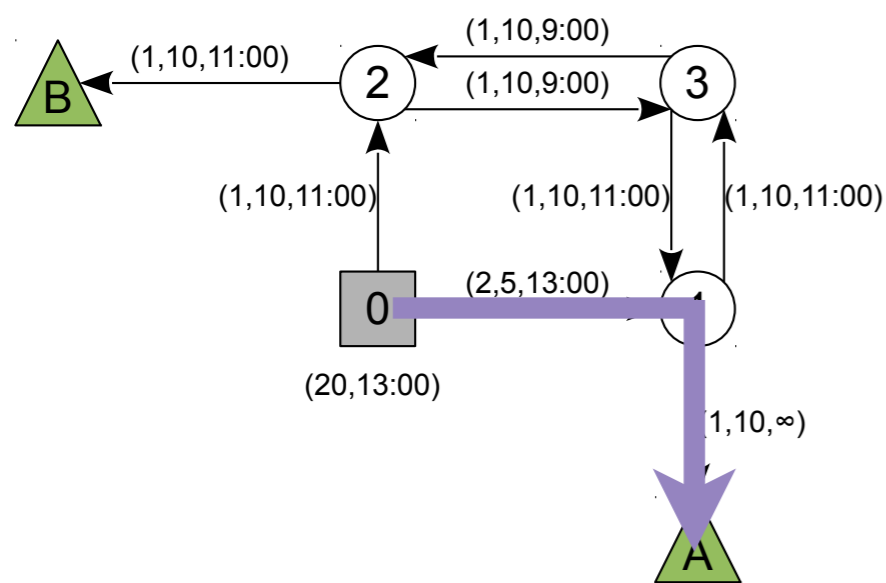
Evacuation route

Evacuation schedule

Evacuation Scheduling

5 leaving at 9:00

5 leaving at 10:00

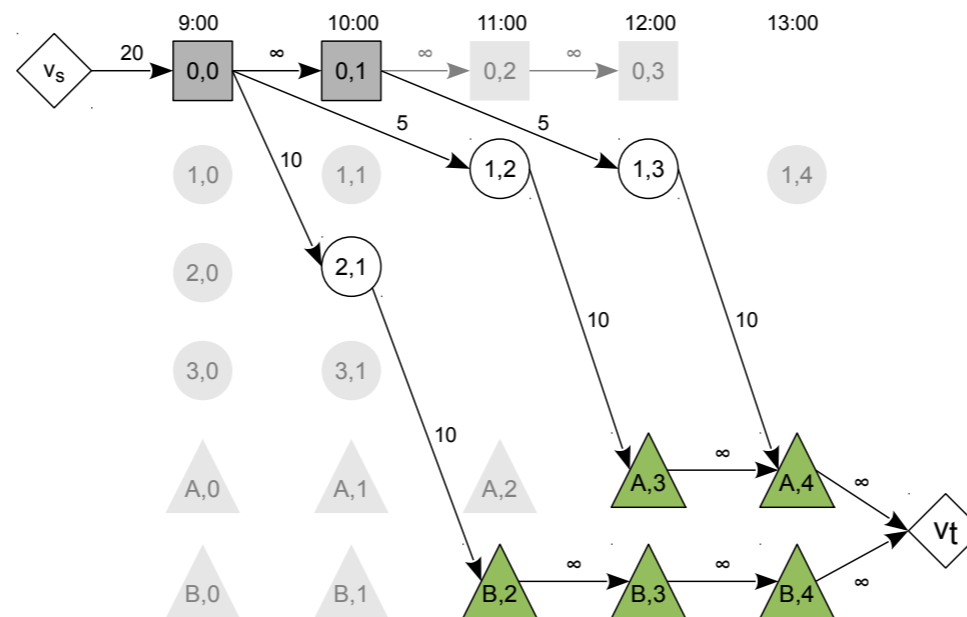


Evacuation route

Evacuation schedule

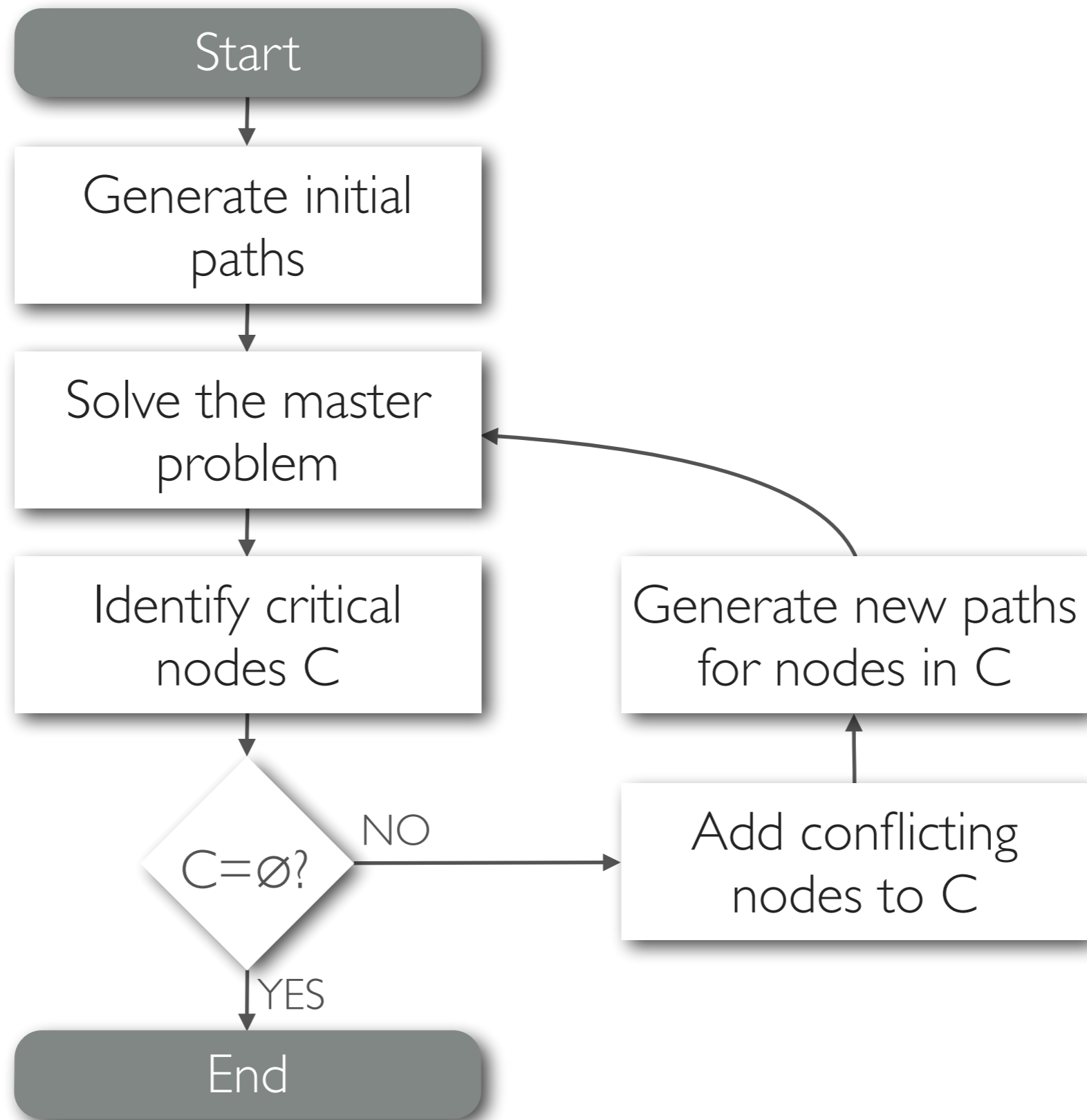
State Of The Art

- Most approaches rely on free flow models
 - Solve a max flow problem on the time-expanded graph

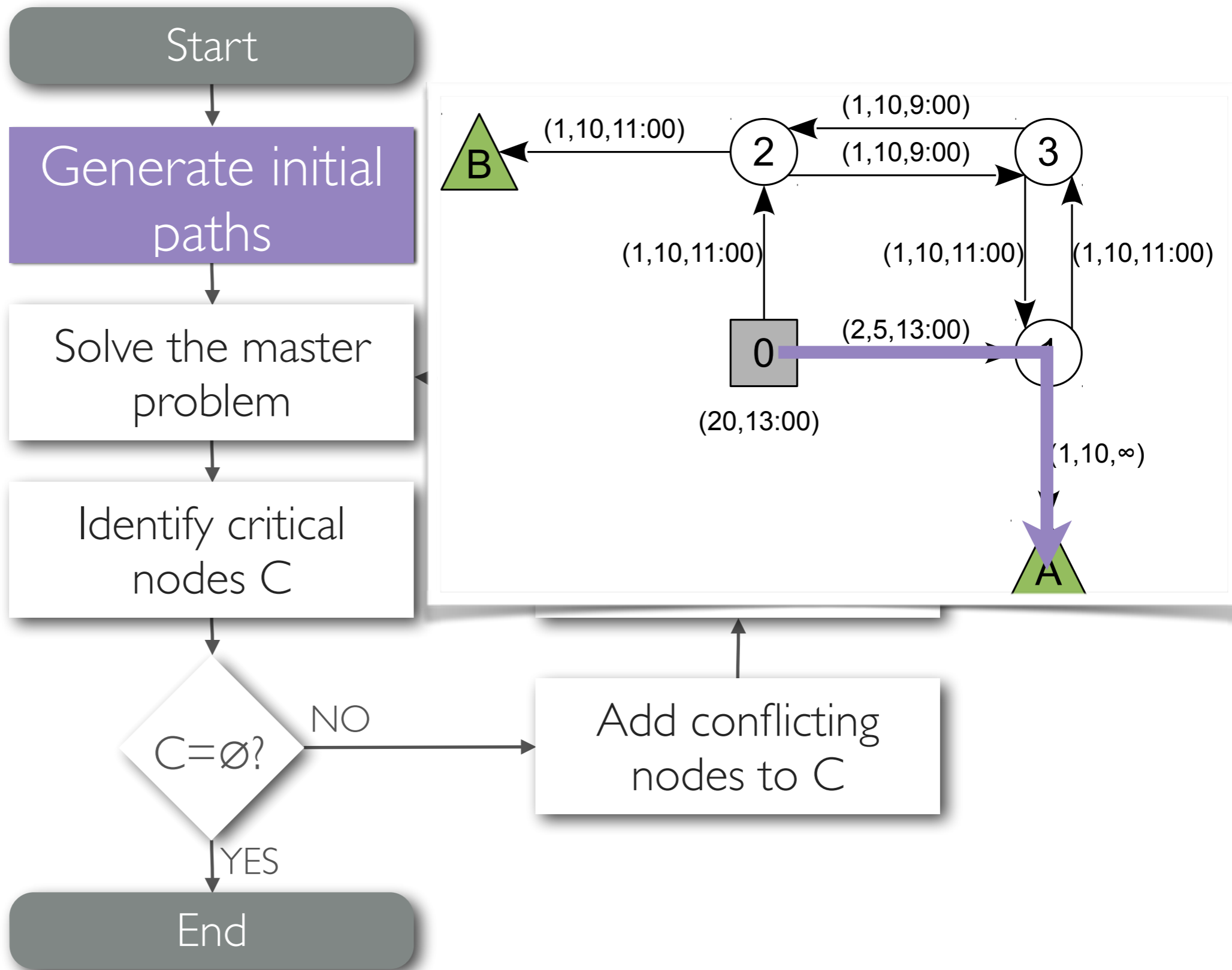


- Limitations
 - No detailed instructions to evacuees (no evacuation route)
 - Underestimate the time required for evacuation

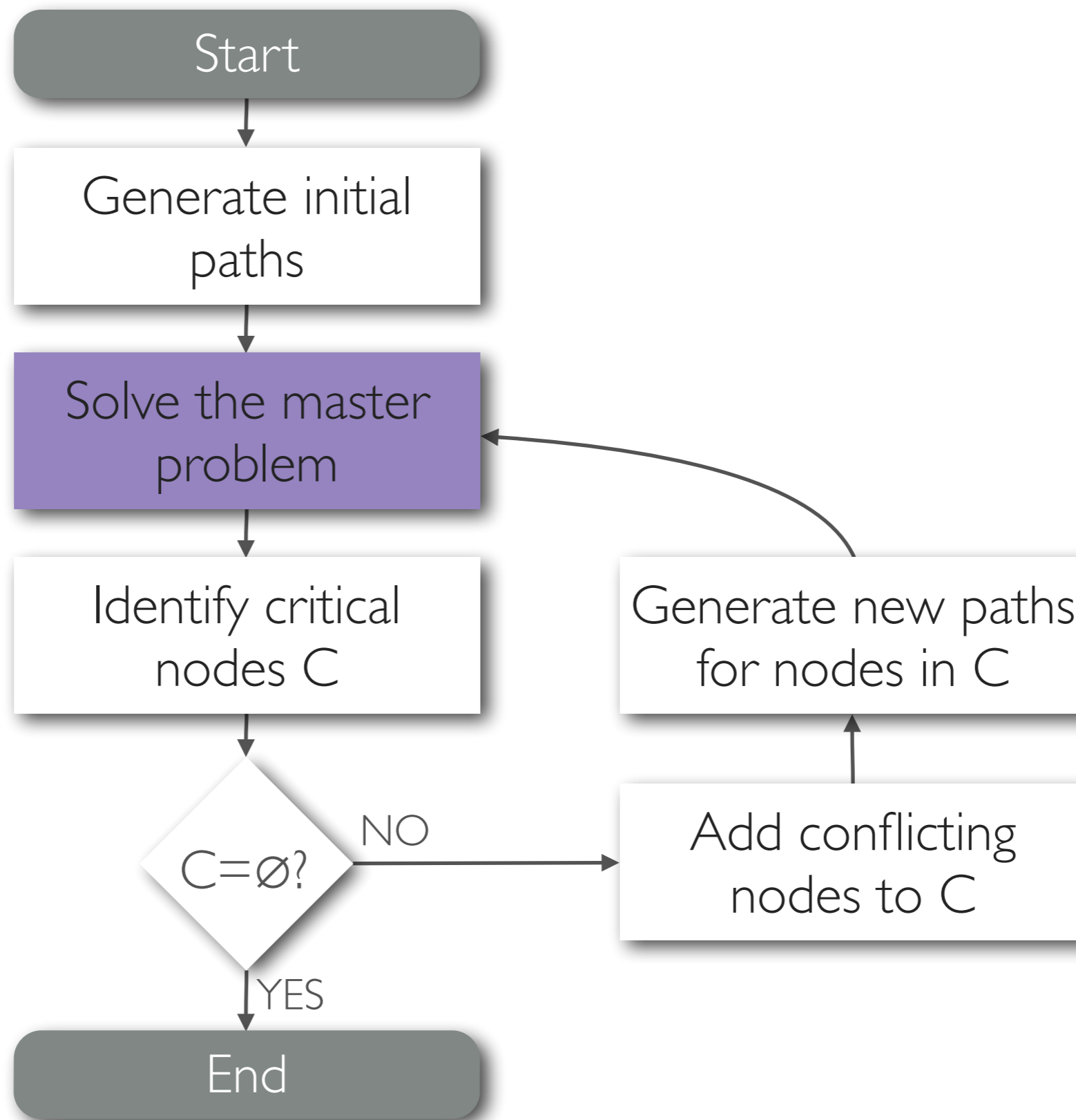
Conflict Path Generation (CPG)



Conflict Path Generation (CPG)



Approach Overview



Reduced Master Problem I

$$\begin{aligned}
 \max \quad & \sum_{p \in \Omega} \sum_{t \in \mathcal{H}_p} \varphi_t^p \\
 \text{s.t.} \quad & \sum_{p \in \Omega_k} x_p = 1 && \forall k \in \mathcal{E} \\
 & \sum_{p \in \Omega_k} \sum_{t \in \mathcal{H}_p} \varphi_p^t + \varphi_k = d_k && \forall k \in \mathcal{E} \\
 & \sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq u_e && \forall e \in \mathcal{A} \setminus \mathcal{A}_c, t \in \mathcal{H} \\
 & \sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq y_e u_e + (1 - y_{\bar{e}}) u_{\bar{e}} && e \in \mathcal{A}_c, t \in \mathcal{H} \\
 & y_e + y_{\bar{e}} \geq 1 && \forall e \in \hat{\mathcal{A}}_c \\
 & y_e \geq x_p && \forall e \in \mathcal{A}_c, \forall p \in \omega(e) \\
 & \sum_{t \in \mathcal{H}_p} \varphi_p^t \leq |\mathcal{H}_p| x_p u_p && \forall p \in \Omega \\
 & \varphi_p^t \geq 0 && \forall p \in \Omega, t \in \mathcal{H}_p \\
 & \varphi_k \geq 0 && \forall k \in \mathcal{E} \\
 & y_e \in \{0, 1\} && \forall e \in \mathcal{A}_c \\
 & x_p \in \{0, 1\} && \forall p \in \Omega
 \end{aligned}$$

Reduced Master Problem I

Max. number of evacuees reaching safety

$$\begin{aligned}
 \max \quad & \sum_{p \in \Omega} \sum_{t \in \mathcal{H}_p} \varphi_t^p \\
 \text{s.t.} \quad & \sum_{p \in \Omega_k} x_p = 1 && \forall k \in \mathcal{E} \\
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 \end{aligned}$$

Reduced Master Problem I

$$\max \sum_{p \in \Omega} \sum_{t \in \mathcal{H}_p} \varphi_t^p$$

Max. number of evacuees reaching safety

$$\text{s.t.} \sum_{p \in \Omega_k} x_p = 1$$

Select one path per evacuated area

$$\sum_{p \in \Omega_k} \sum_{t \in \mathcal{H}_p} \varphi_p^t + \varphi_k = d_k$$

$$\forall k \in \mathcal{E}$$

$$\sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq u_e$$

$$\forall e \in \mathcal{A} \setminus \mathcal{A}_c, t \in \mathcal{H}$$

$$\sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq y_e u_e + (1 - y_{\bar{e}}) u_{\bar{e}}$$

$$e \in \mathcal{A}_c, t \in \mathcal{H}$$

$$y_e + y_{\bar{e}} \geq 1$$

$$\forall e \in \hat{\mathcal{A}}_c$$

$$y_e \geq x_p$$

$$\forall e \in \mathcal{A}_c, \forall p \in \omega(e)$$

$$\sum_{t \in \mathcal{H}_p} \varphi_p^t \leq |\mathcal{H}_p| x_p u_p$$

$$\forall p \in \Omega$$

$$\varphi_p^t \geq 0$$

$$\forall p \in \Omega, t \in \mathcal{H}_p$$

$$\varphi_k \geq 0$$

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$$\forall e \in \mathcal{A}_c$$

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Reduced Master Problem I

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Max. number of evacuees reaching safety

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Select one path per evacuated area

$$\sum_{p \in \Omega_k} \sum_{t \in \mathcal{H}_p} \varphi_p^t + \varphi_k = d_k$$

Account for non evacuated vehicles

$$\sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq u_e$$

$$\forall e \in \mathcal{A} \setminus \mathcal{A}_c, t \in \mathcal{H}$$

$$\sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq y_e u_e + (1 - y_{\bar{e}}) u_{\bar{e}}$$

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$$\sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq y_e u_e + (1 - y_{\bar{e}}) u_{\bar{e}}$$

$$y_e + y_{\bar{e}} \geq 1$$

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$$\varphi_p^t \geq 0$$

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$$y_e \in \{0, 1\}$$

$$x_p \in \{0, 1\}$$

Max. number of evacuees reaching safety

Select one path per evacuated area

Account for non evacuated vehicles

Edge capacity
&
Contraflow decisions

$$\forall e \in \mathcal{A}_c, \forall p \in \omega(e)$$

$$\forall p \in \Omega$$

$$\forall p \in \Omega, t \in \mathcal{H}_p$$

$$\forall k \in \mathcal{E}$$

$$\forall e \in \mathcal{A}_c$$

$$\forall p \in \Omega$$

Reduced Master Problem I

$$\max \sum_{p \in \Omega} \sum_{t \in \mathcal{H}_p} \varphi_p^t$$

Max. number of evacuees reaching safety

$$\text{s.t. } \sum_{p \in \Omega_k} x_p = 1$$

Select one path per evacuated area

$$\sum_{p \in \Omega_k} \sum_{t \in \mathcal{H}_p} \varphi_p^t + \varphi_k = d_k$$

Account for non evacuated vehicles

$$\sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq u_e$$

Edge capacity
&
Contraflow decisions

$$\sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq y_e u_e + (1 - y_{\bar{e}}) u_{\bar{e}}$$

$$y_e + y_{\bar{e}} \geq 1$$

$$y_e \geq x_p$$

$$\forall e \in \mathcal{A}_c, \forall p \in \omega(e)$$

$$\sum_{t \in \mathcal{H}_p} \varphi_p^t \leq |\mathcal{H}_p| x_p u_p$$

Link flow and path selection variables

$$\varphi_p^t \geq 0$$

$$\forall p \in \Omega, t \in \mathcal{H}_p$$

$$\varphi_k \geq 0$$

$$\forall k \in \mathcal{E}$$

$$y_e \in \{0, 1\}$$

$$\forall e \in \mathcal{A}_c$$

$$x_p \in \{0, 1\}$$

$$\forall p \in \Omega$$

Reduced Master Problem I

$$\begin{aligned}
 \max \quad & \sum_{p \in \Omega} \sum_{t \in \mathcal{H}_p} \varphi_t^p \\
 \text{s.t.} \quad & \sum_{p \in \Omega_k} x_p = 1 \\
 & \sum_{p \in \Omega_k} \sum_{t \in \mathcal{H}_p} \varphi_p^t + \varphi_k \\
 & \sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq y_e \\
 & \sum_{\substack{p \in \omega(e) \\ t - \tau_p^e \in \mathcal{H}_p}} \varphi_p^{t - \tau_p^e} \leq y_{\bar{e}} \\
 & y_e + y_{\bar{e}} \geq 1 \\
 & y_e \geq x_p \\
 & \sum_{t \in \mathcal{H}_p} \varphi_p^t \leq |\mathcal{H}_p| x_p u_p \\
 & \varphi_p^t \geq 0 \\
 & \varphi_k \geq 0 \\
 & y_e \in \{0, 1\} \\
 & x_p \in \{0, 1\}
 \end{aligned}$$

Max. number of evacuees reaching safety

Select one path per evacuated area

Advantages:

- Adds variables and constraints only when needed
- Factor 100 reduction in number of variables and constraints

Link flow and path selection variables

$$\forall e \in \mathcal{A}_c, \forall p \in \omega(e)$$

$$\forall p \in \Omega, t \in \mathcal{H}_p$$

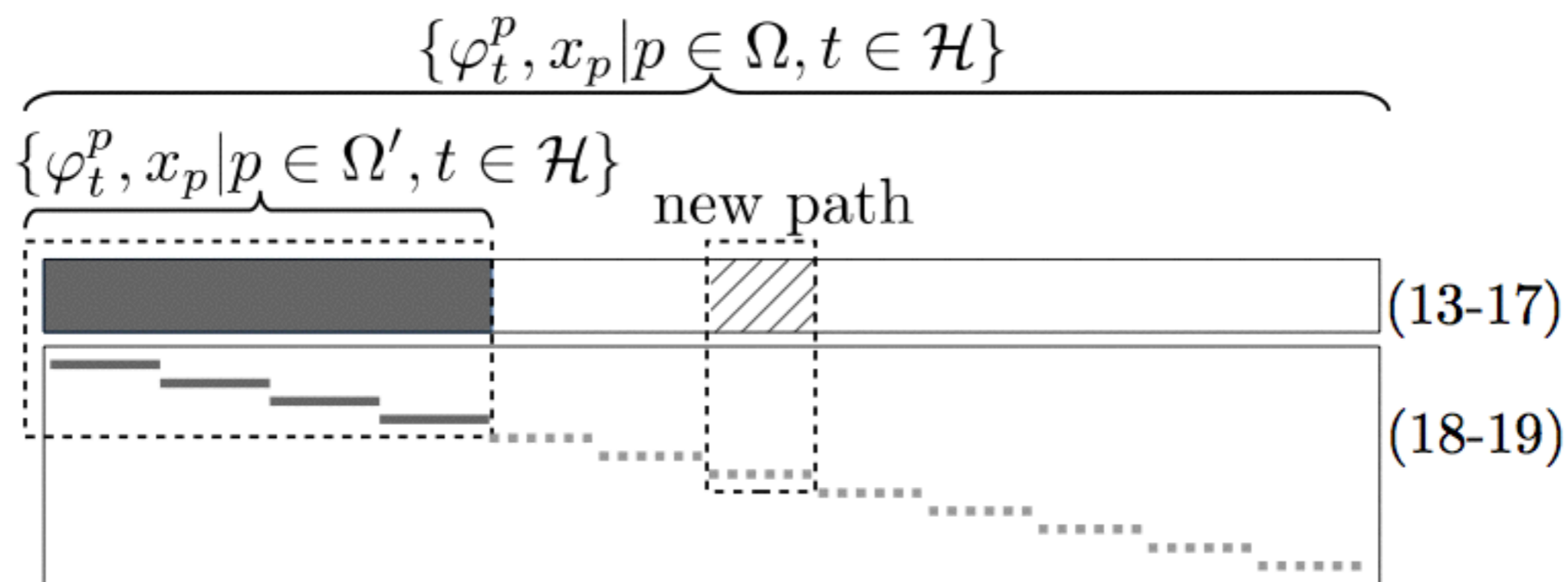
$$\forall k \in \mathcal{E}$$

$$\forall e \in \mathcal{A}_c$$

$$\forall p \in \Omega$$

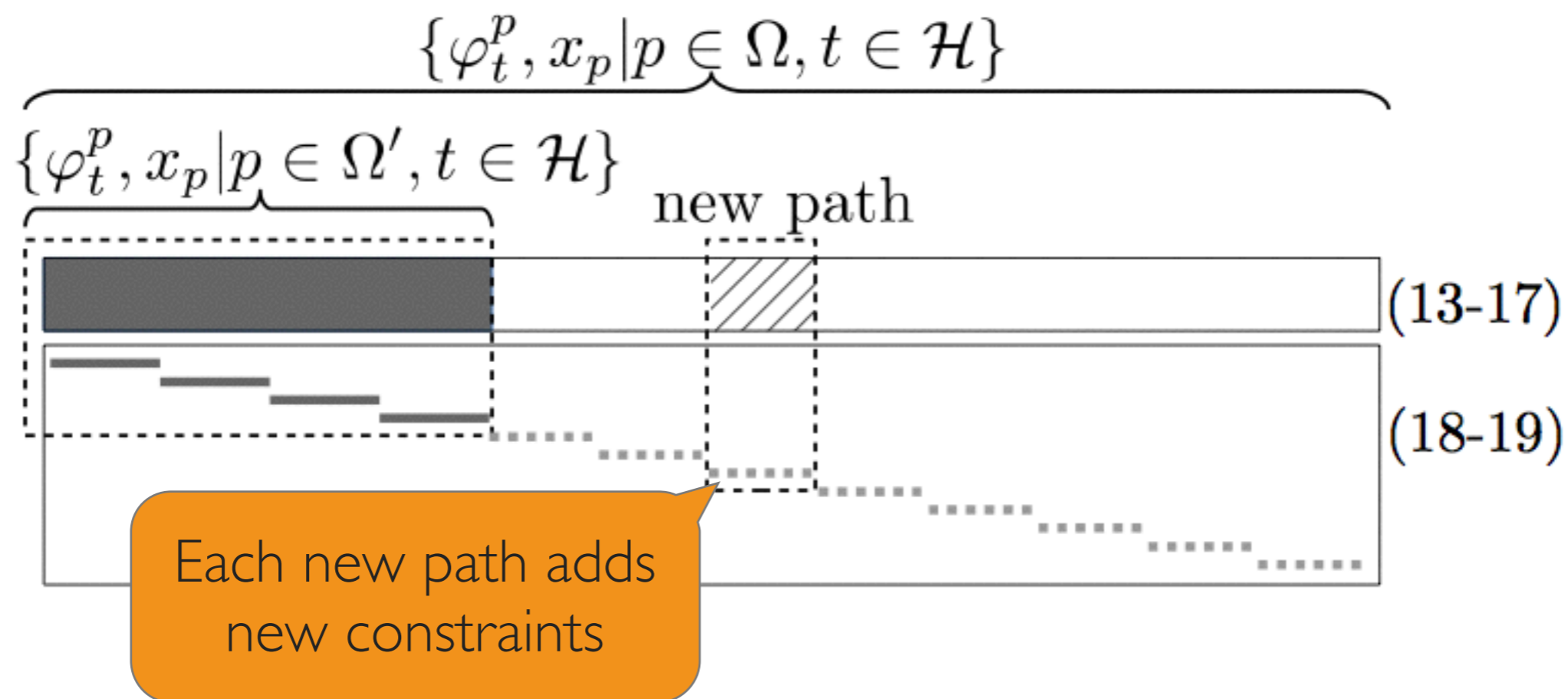
Reduced Master Problem 2

- Structure of the master problem:

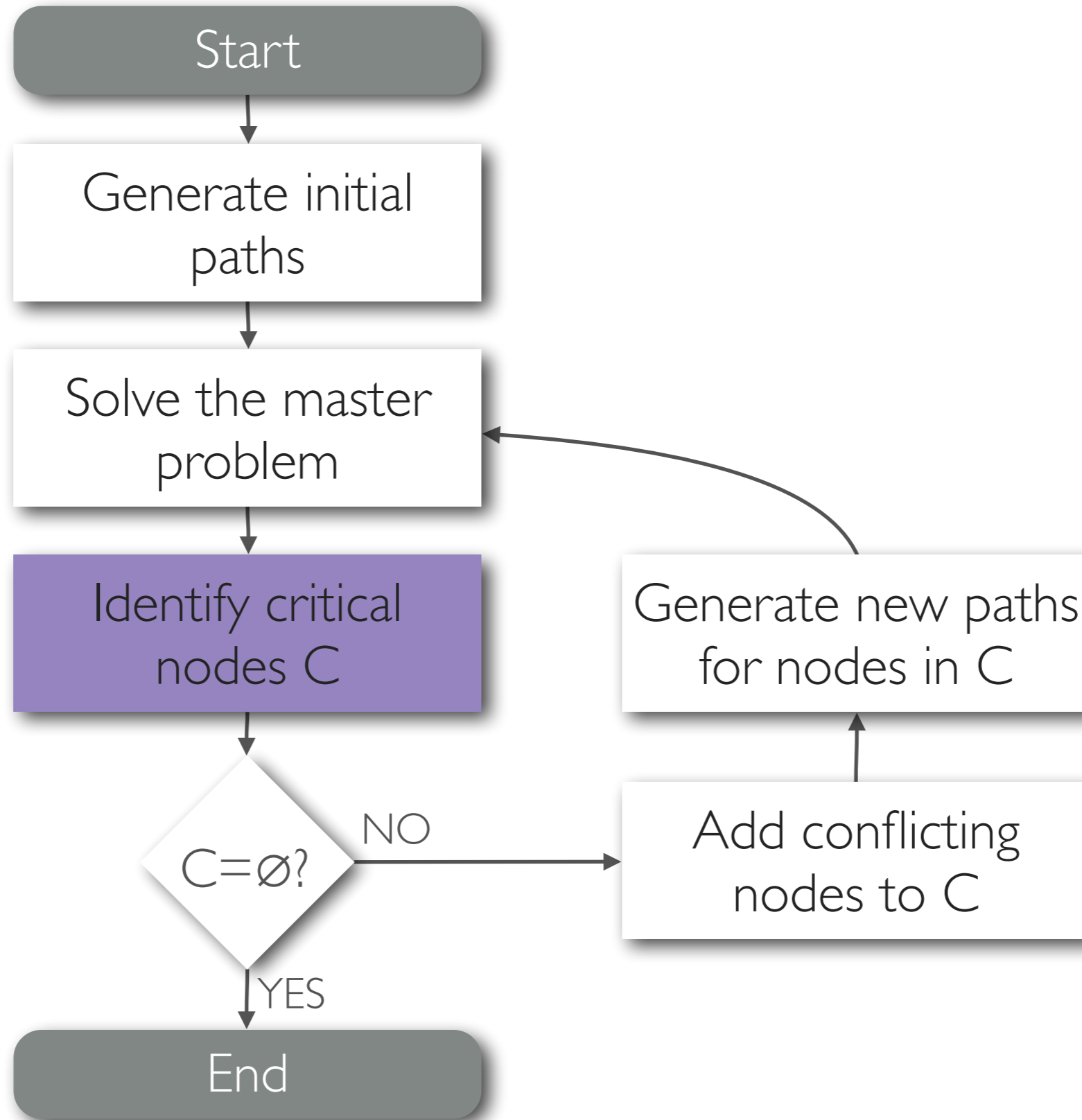


Reduced Master Problem 2

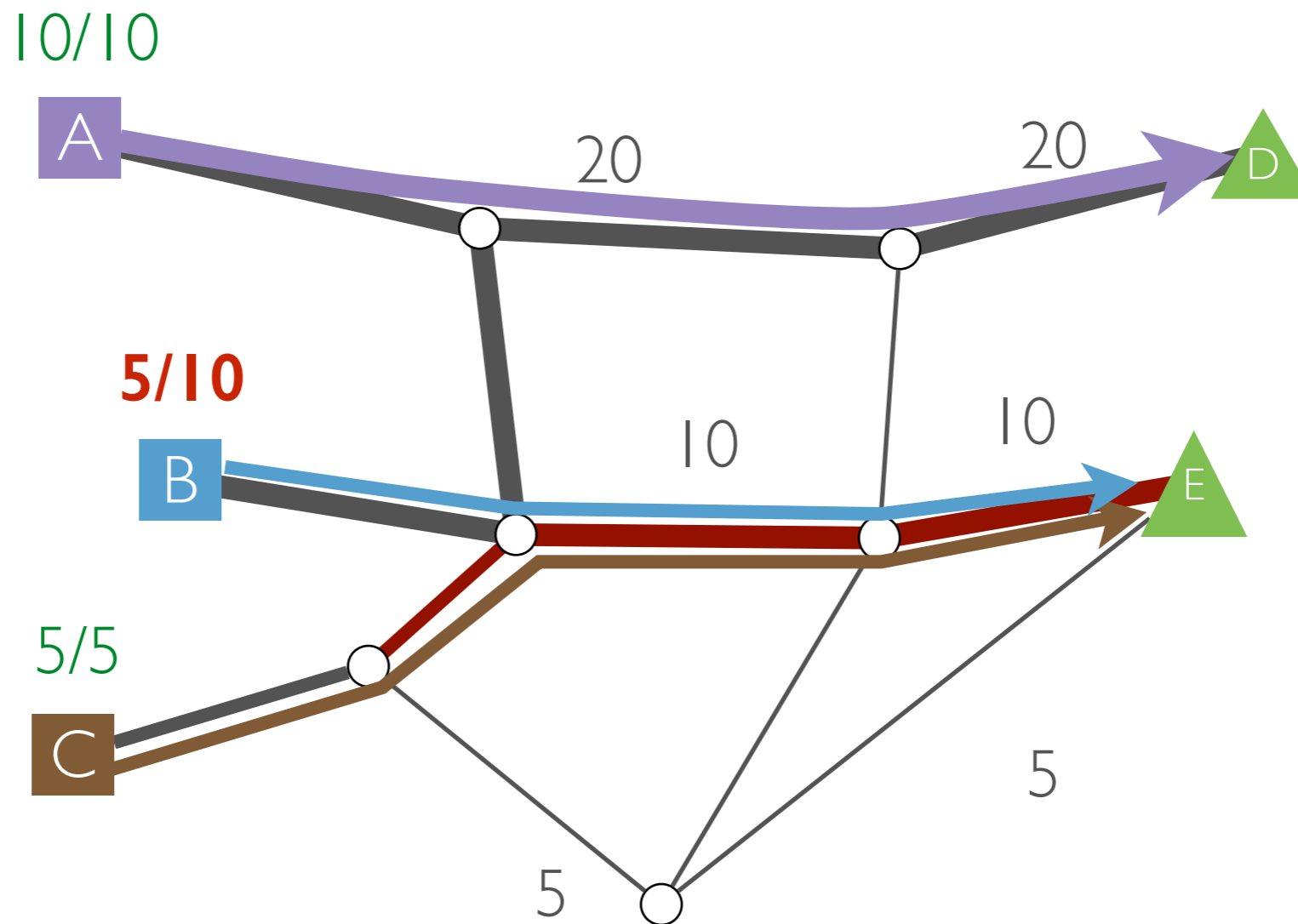
- Structure of the master problem:



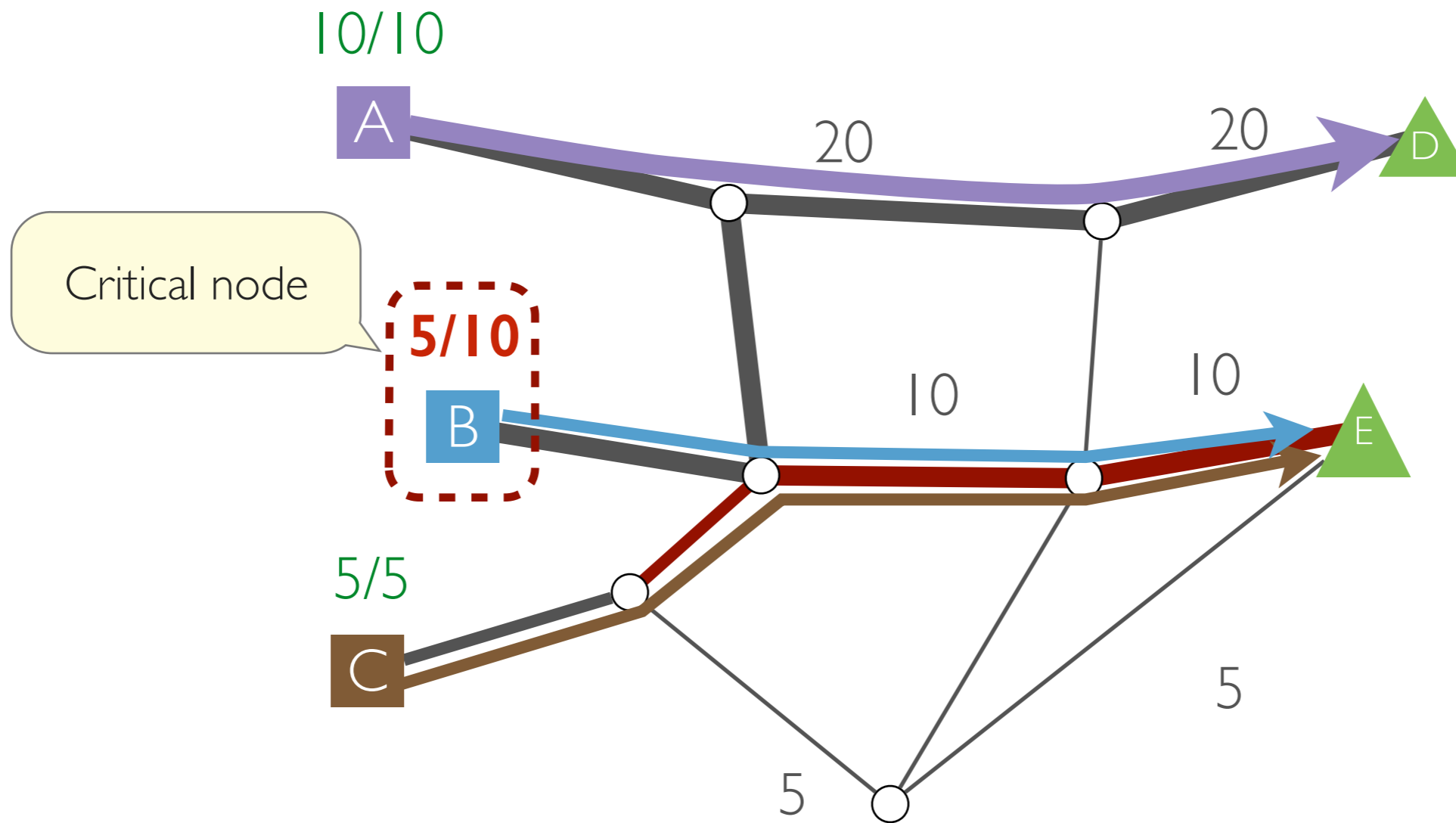
Approach Overview



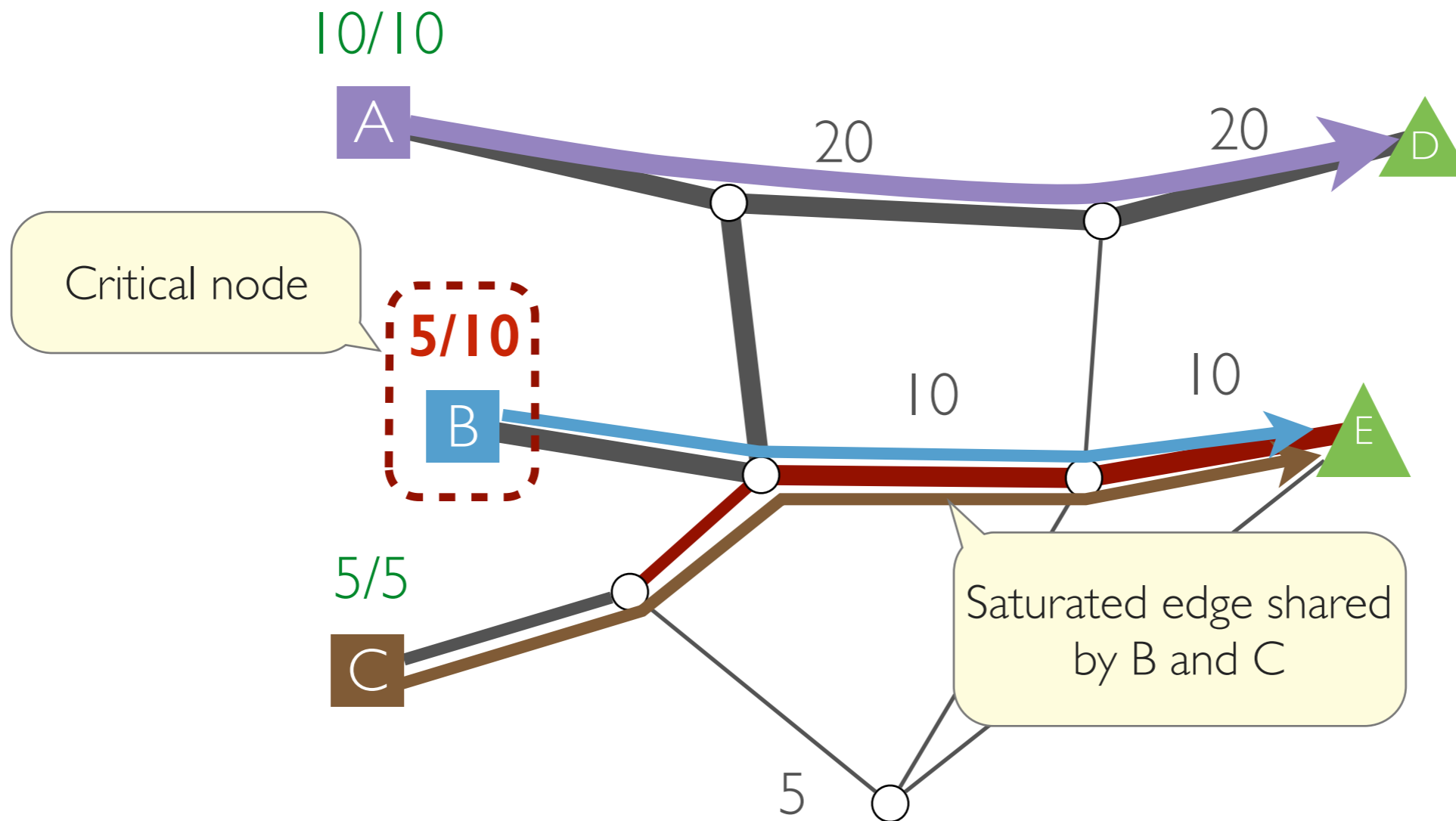
Critical Evacuated Nodes



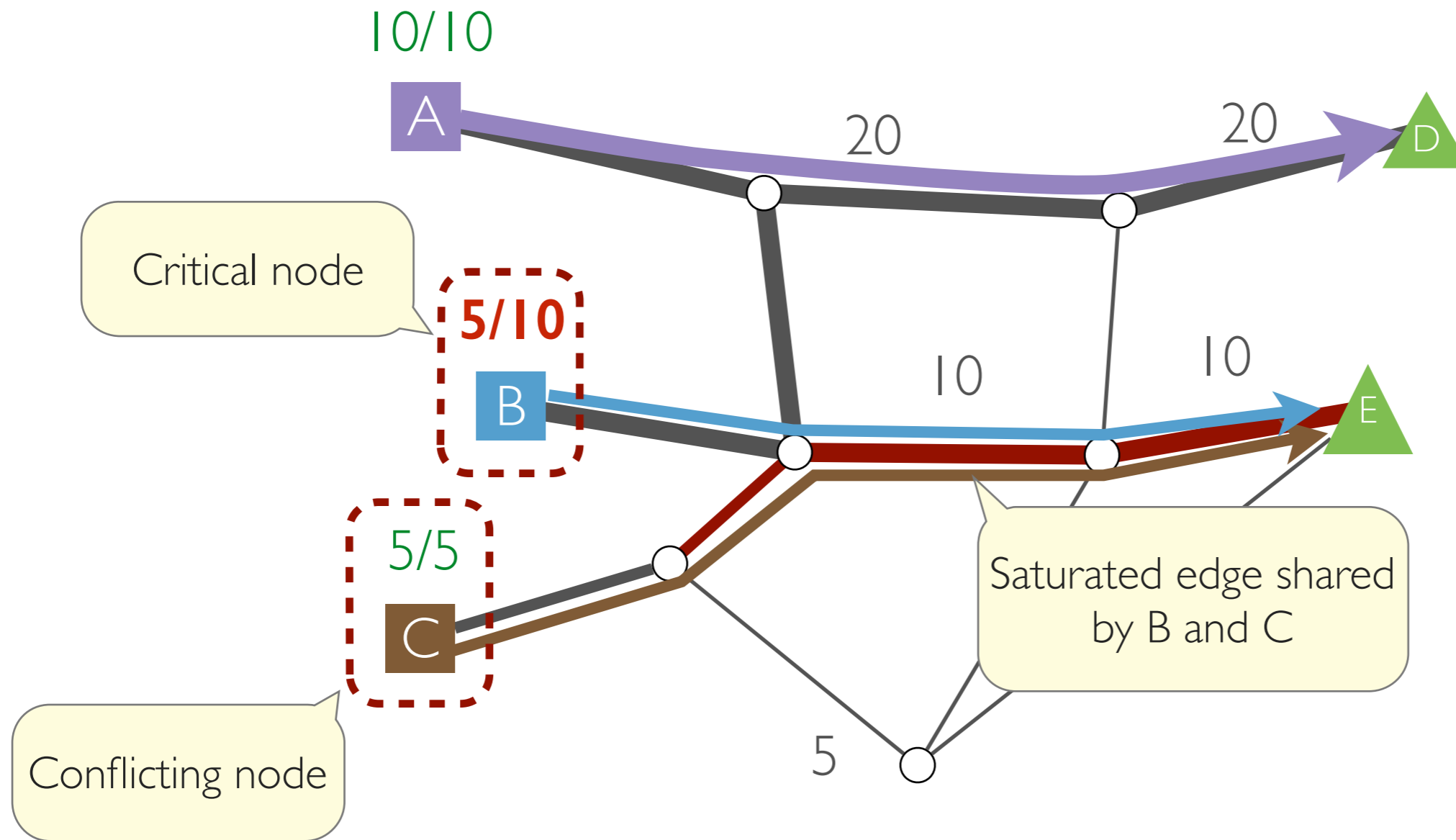
Critical Evacuated Nodes



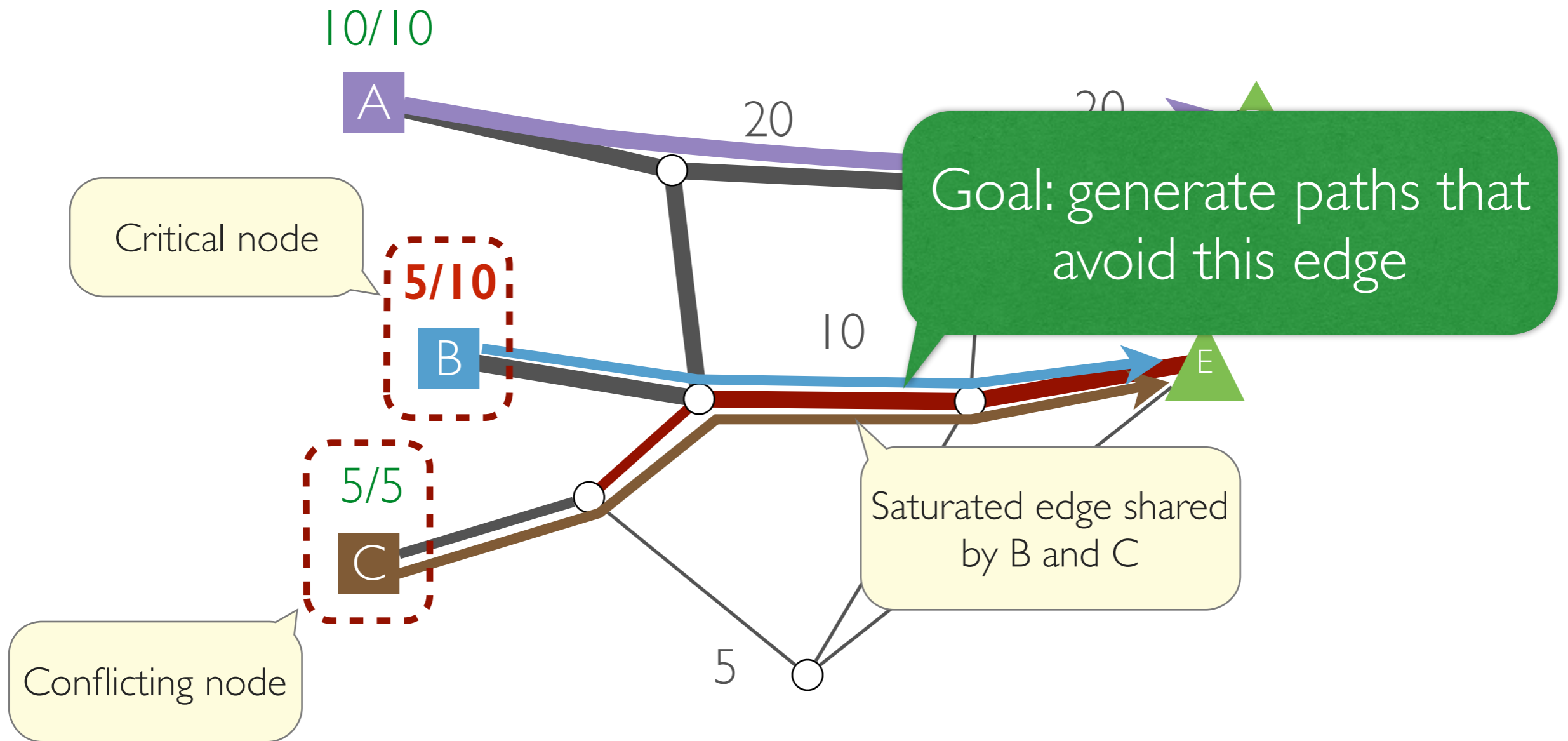
Critical Evacuated Nodes



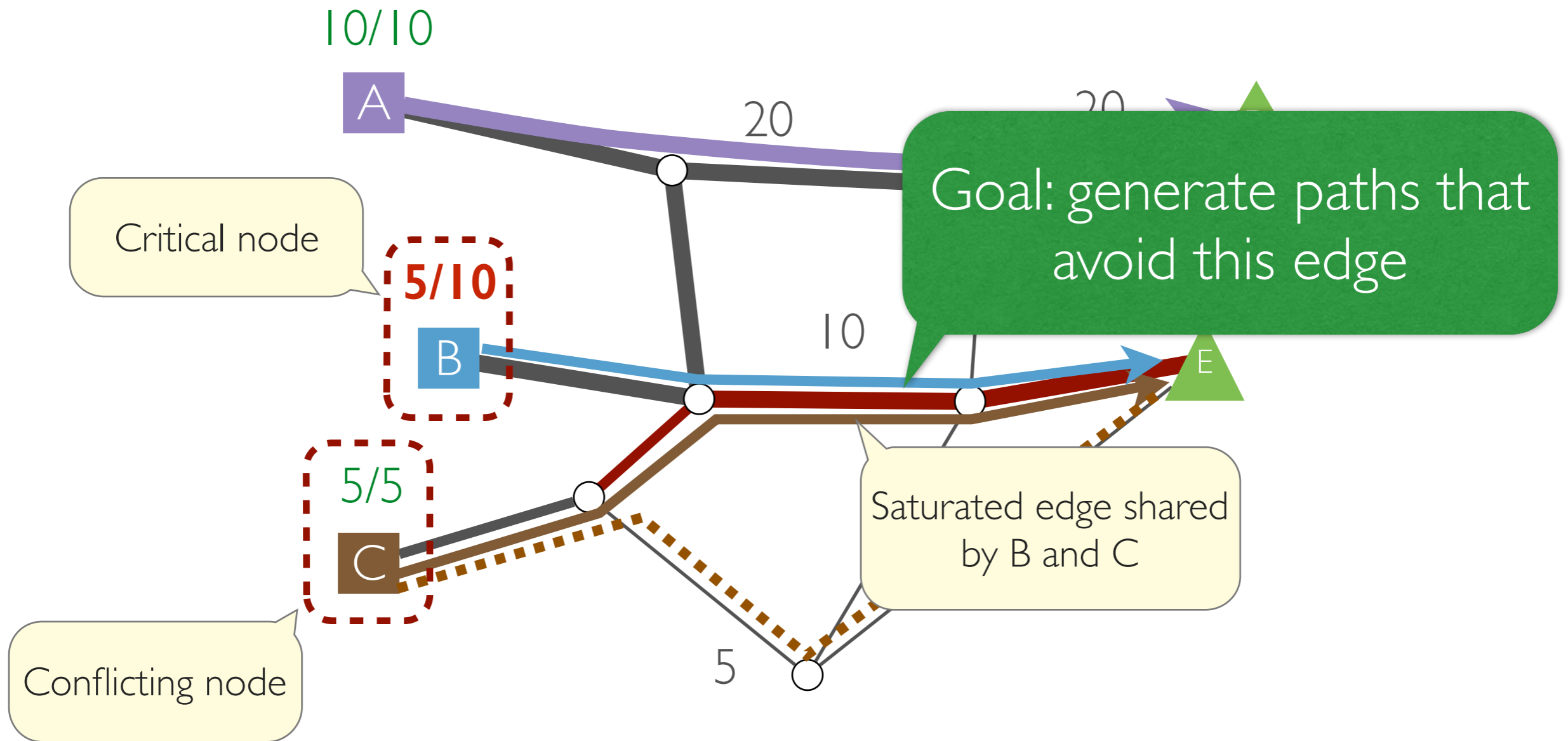
Critical Evacuated Nodes



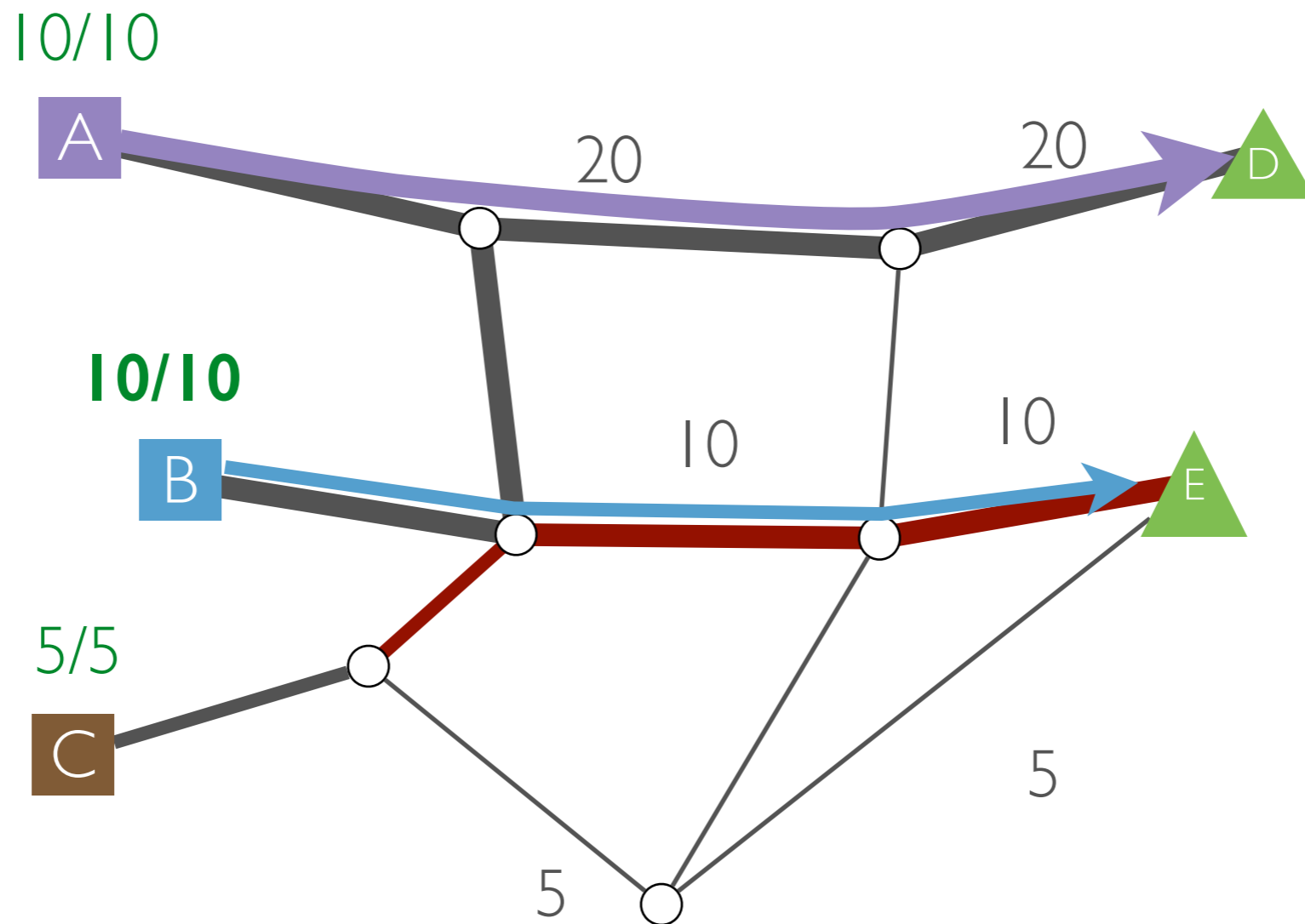
Critical Evacuated Nodes



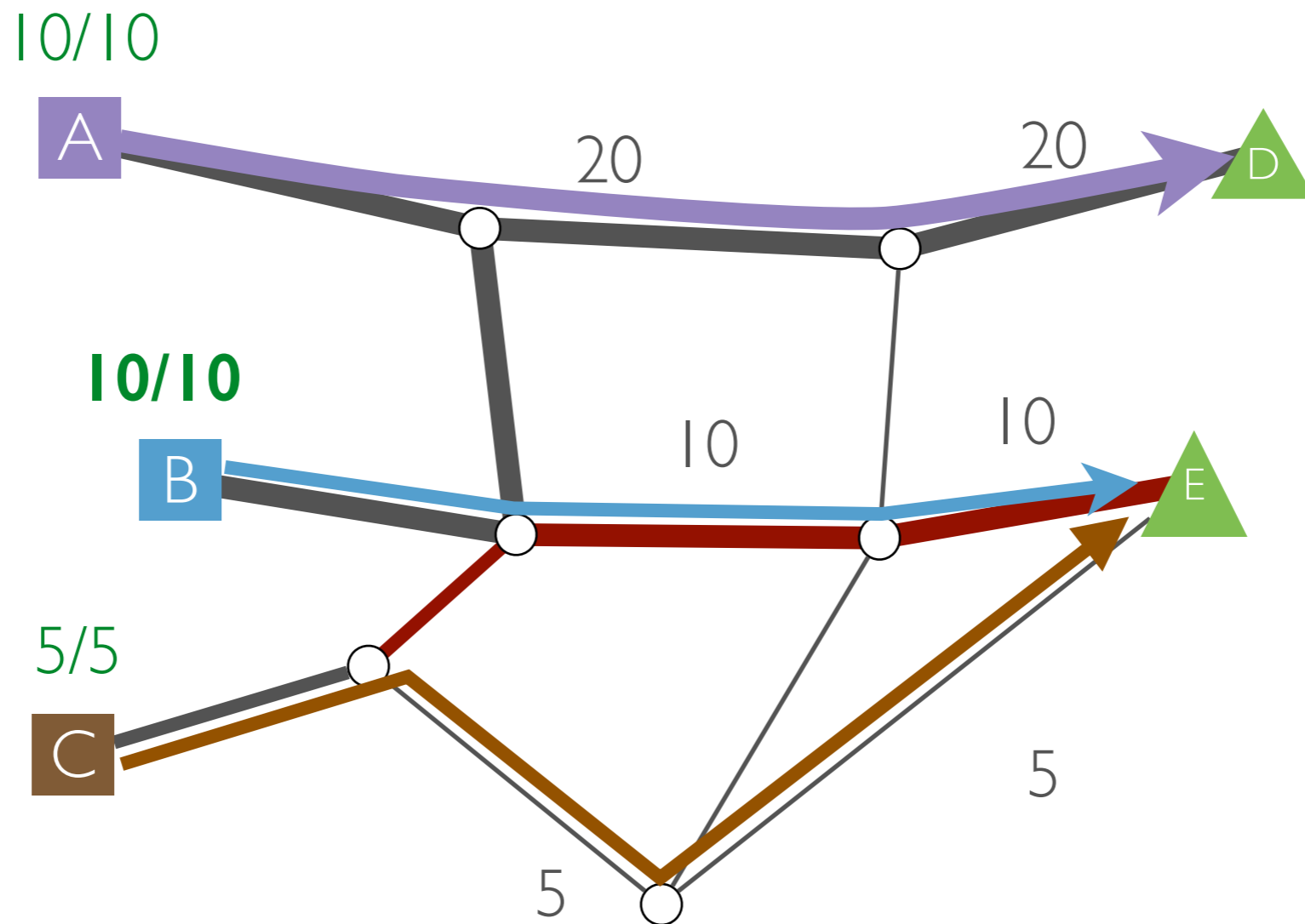
Critical Evacuated Nodes



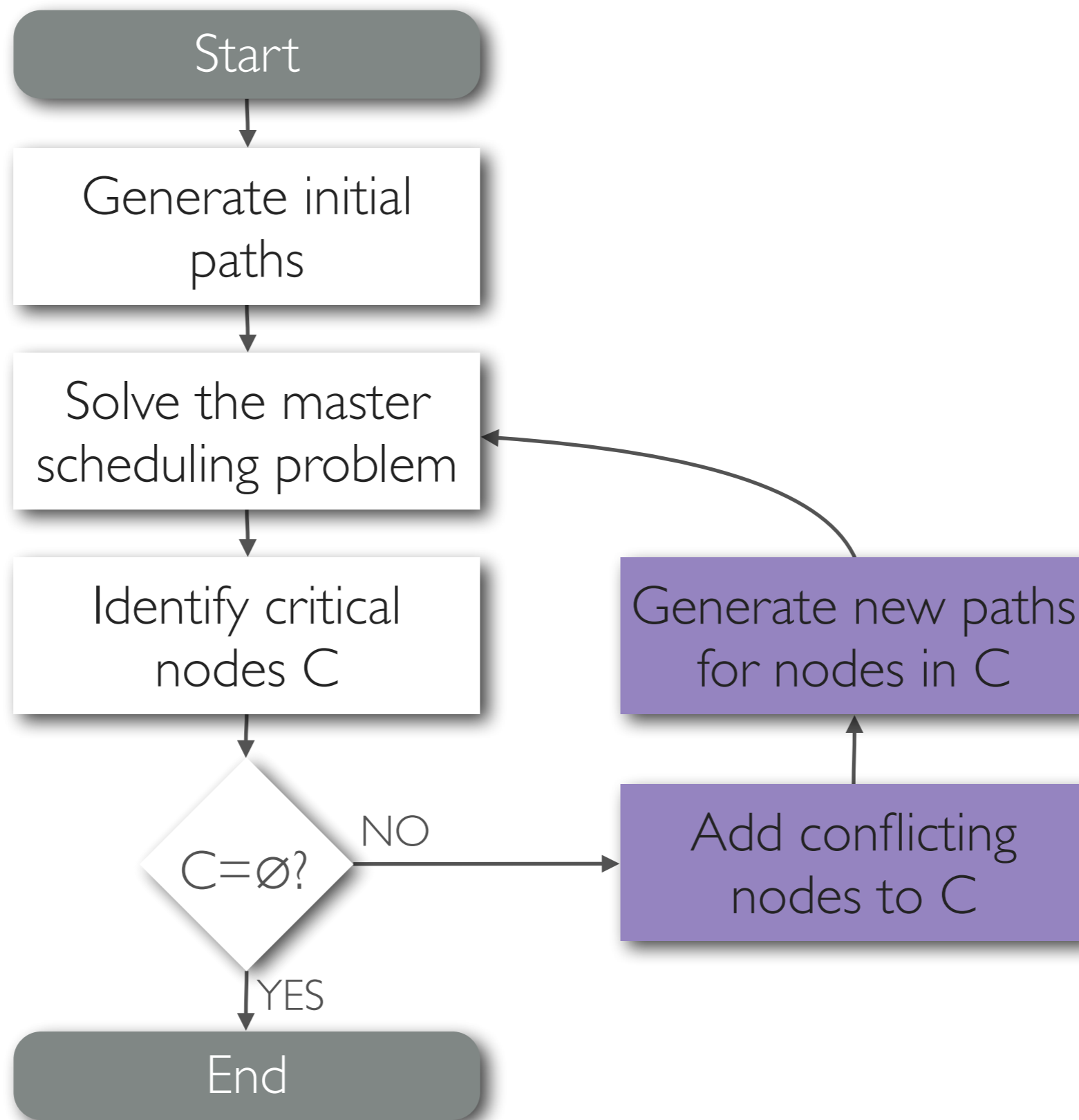
Critical Evacuated Nodes



Critical Evacuated Nodes



Approach Overview



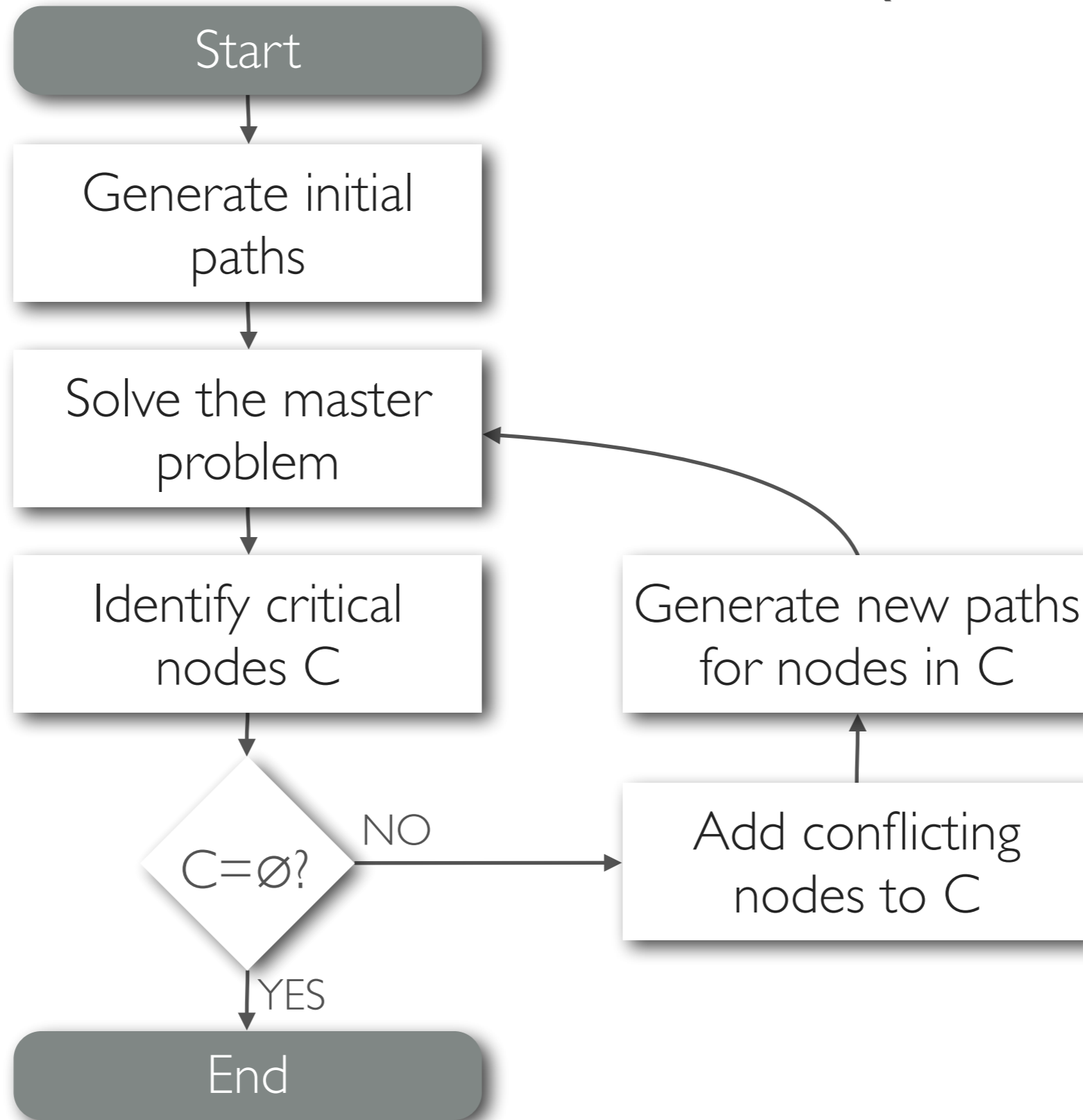
Heuristic Path Generation (HPG)



- Generate paths without considering the evacuation schedule
- Shortest path in the evacuation graph
- Penalize edges depending on current solution



Conflict Path Generation (CPG)

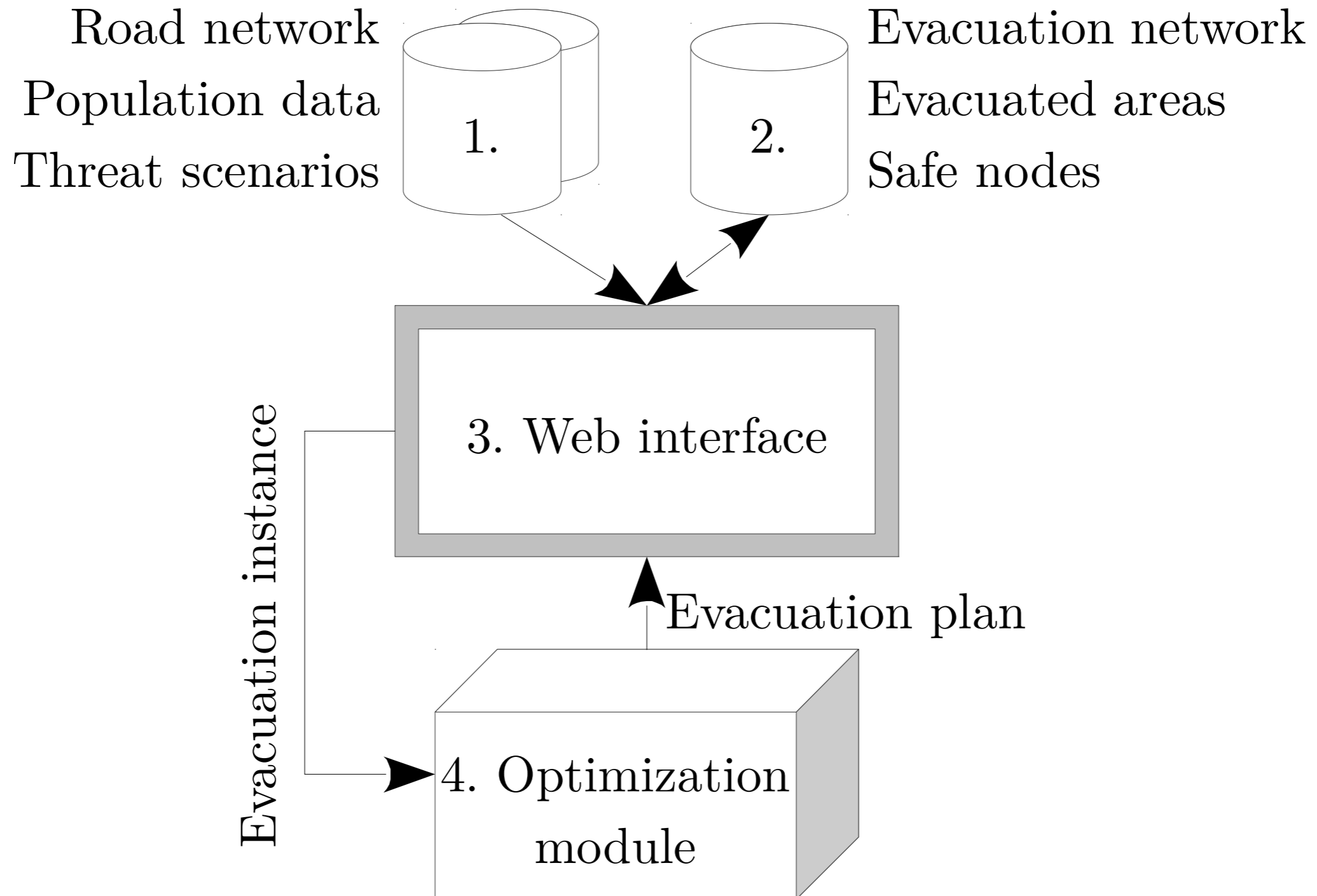


Computational experiments



Instance	Contraflow	Num. evac.	Num. nodes	Num. paths	CPU (min)	Perc. Evac.	Evac. Time
Hawkesbury Nepean	No	70k	170	1014	15	100%	8h05
	Yes	70k	170	1125	6	100%	5h34
New Orleans	No	1m	2000	3741	131	100%	60h48
	Yes	1m	2000	3818	152	100%	39h53

NICTA Evacuation Planner



NICTA Evacuation Planner



The screenshot shows the NICTA Evacuation Planner web application. A "Select Project" dialog box is centered on the screen, featuring three radio button options: "Canberra", "New Orleans", and "Hawkesbury Nepean". A blue "Confirm" button is located at the bottom right of the dialog. The background is a map of New York City and surrounding areas, including labels for Newark, Elizabeth, and New Brunswick. The interface includes a top navigation bar with "NICTA Evacuations" and "Switch Project", a search bar, and a left sidebar with "Layers" and "Basemap" sections. The "Basemap" section has three options: "Streets" (selected), "Imagery", and "Hybrid". A status bar at the bottom left shows "Waiting for developer.mapquest.com..." and the bottom right contains map data attribution for Leaflet, MapQuest, and OpenStreetMap.

NICTA Evacuation Planner



A screenshot of the NICTA Evacuation Planner web application. The interface features a dark header with the title "NICTA Evacuations" and a "Switch Project" button. On the left, there is a sidebar with "Layers" and "Basemap" sections. The "Basemap" section has three radio buttons: "Streets" (selected), "Imagery", and "Hybrid". A search bar is located in the top right corner. A white "Select Project" dialog box is centered on the screen, containing three radio button options: "Canberra", "New Orleans", and "Hawkesbury Nepean". A blue "Confirm" button is at the bottom right of the dialog. The background is a map of New York City and surrounding areas, showing major highways and city names like Newark, Elizabeth, and New Brunswick. A status bar at the bottom left shows "Waiting for developer.mapquest.com..." and the bottom right has map data attribution for Leaflet, MapQuest, and OpenStreetMap.

Take away

- Evacuations are a critical aspect of disaster management
 - Evacuation planners heavily rely on expert knowledge
 - Decision support systems are needed!
- Conflict based path generation
 - General decomposition approach
 - Leverage domain knowledge to generate new columns
 - Useful when the Master Problem is a MIP

Perspectives

- Current work
 - Include evacuees behavior in optimization
 - Traditional column generation approach
 - Refine modeling of the road network
 - Deploy with an emergency service partner
- Extensions
 - Model operational cost of contraflow
 - Agent based simulation including behaviors